

$e^+ e^-$ annihilation cross section, $\sigma = (20.8 \text{ nb} \cdot \text{GeV}^2 / 4s) \int \int (1 + \cos^2 \theta^*) d(\cos \theta^*) d\phi$,

where,

$s = (\text{center of mass energy})^2 = W^2 = 4(E_b^*)^2 = (2m_\mu)^2$ at threshold

$W =$ total energy in the system

$E_b^* =$ center of mass beam energy

$\theta^* =$ center of mass polar angle $\Rightarrow 0$ to π

$\phi =$ azimuthal angle $\Rightarrow 0$ to 2π

In lab: $W = \sqrt{2E_{\text{beam}} m_e}$, so at threshold, $E_{\text{beam}} = (2m_\mu)^2 / 2m_e = 43.7 \text{ GeV}$

Integrating over ϕ ,

$$\sigma = \underbrace{(2\pi \cdot 20.8 \text{ nb} \cdot \text{GeV}^2 / 16(E_b^*)^2)}_{8.168 / (E_b^*)^2 \text{ nb}} \underbrace{\int (1 + \cos^2 \theta^*) d(\cos \theta^*)}_{2 \text{ \%}}$$

$8.168 / (E_b^*)^2 \text{ nb}$

$2 \text{ \%$

At $E_{\text{beam}} = 43.7 \text{ GeV}$,

$$E_b^* = m_\mu = 0.1056 \text{ GeV}, \sigma_{\text{tot}} = 1.9 \times 10^{-30} \text{ cm}^2$$