



# Advanced Geometry

FLUKA Beginner's Course

# Contents

- body transformations
- lattice
- voxels

# Geometry directives

Special commands enclosing body definition:

`$Start_xxx`

.....

`$End_xxx`

where "xxx" stands for  
"expansion", "translat" or "transform"

They provide respectively a coordinate **expansion/reduction**, a coordinate **translation** or a coordinate **roto-translation** of the bodies embedded between the starting and the ending directive lines.

# Directives in geometry: expansion/reduction

➤ `$Start_expansion ... $End_expansion`

it provides a coordinate expansion (reduction) factor **f** for all bodies embedded within the directive

`$Start_expansion 10.0`

`SPH Sphere 5.0 7.0 8.0 50.0`

`$End_expansion`

transforms a sphere of radius 50 centered in (+5,+7,+8) into a sphere of radius 500 centered in (+50,+70,+80)

Putting the body in its quadric form

$$A_{xx}x^2 + A_{yy}y^2 + A_{zz}z^2 + A_{xy}xy + A_{xz}xz + A_{yz}yz + A_x x + A_y y + A_z z + A_0 = 0$$

$$\text{or } \begin{bmatrix} x & y & z & 1 \end{bmatrix} \begin{bmatrix} A_{xx} & A_{xy}/2 & A_{xz}/2 & A_x/2 \\ A_{xy}/2 & A_{yy} & A_{yz}/2 & A_y/2 \\ A_{xz}/2 & A_{yz}/2 & A_{zz} & A_z/2 \\ A_x/2 & A_y/2 & A_z/2 & A_0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = 0 \quad \text{i.e.} \quad \mathbf{r}^T \mathbf{M}_{\text{QUA}} \mathbf{r} = 0$$

the expansion/reduction matrix is  $\mathbf{T} = \begin{bmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & f & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$

and the transformed body equation is  $\mathbf{r}^T (\mathbf{T}^{-1})^T \mathbf{M}_{\text{QUA}} \mathbf{T}^{-1} \mathbf{r} = 0$

# Directives in geometry: translation

➤ `$Start_translat ... $End_translat`

it provides a coordinate translation  $S_x, S_y, S_z$  for all bodies embedded within the directive

```
$Start_translat -5.0 -7.0 -8.0
```

```
SPH Sphere 5.0 7.0 8.0 50.0
```

```
$End_translat
```

transforms a sphere of radius 50 centered in (+5,+7,+8)  
into a sphere of radius 50 centered in (0,0,0)

the translation matrix is  $T =$

$$\begin{bmatrix} 1 & 0 & 0 & S_x \\ 0 & 1 & 0 & S_y \\ 0 & 0 & 1 & S_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# Directives in geometry: roto-translation

➤ `$Start_transform ... $End_transform`

it applies a pre-defined (via **ROT-DEFI**) roto-translation to all bodies embedded within the directive

```
ROT-DEFI , 201.0, 0., +116.5650511770780, 0., 0., 0., cylrot
```

```
$Start_transform cylrot
```

```
QUA Cylinder 0.5 1.0 0.5 0.0 1.0 0.0 0.0 0.0 0.0 -4.0
```

```
$End_transform
```

transforms an infinite circular cylinder of radius 2 with axis  $\{x=-z, y=0\}$  into an infinite circular cylinder of radius 2 with axis  $\{x=z/3, y=0\}$  (**clockwise rotation**)

the roto-translation matrix is  $T = \begin{bmatrix} & & & S_x \\ & R & & S_y \\ & & & S_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$

$$T^{-1} = \begin{bmatrix} & & & -(R^{-1}S)_x \\ & R^{-1} & & -(R^{-1}S)_y \\ & & & -(R^{-1}S)_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- it allows to rotate a **RPP** avoiding the use of the deprecated **BOX** !

- note that also the **inverse** transformation can be used  $T^{-1}$

```
$Start_transform -cylrot
```

# ROT-DEFIni

The **ROT-DEFIni** card defines roto-translations that can be applied, in addition to bodies, to i. **USRBIN & EVENTBIN** and ii. **LATTICE**. It transforms the position of the tracked particle i. before scoring with respect to the defined binning or ii. into the prototype with the order:

- First applies the **translation**
- followed by the rotation on the **azimuthal angle**
- and finally by the rotation on the **polar angle**.

$$\mathbf{X}_{\text{new}} = \mathbf{M}_{\text{polar}} \times \mathbf{M}_{\text{az}} \times (\mathbf{X} + \mathbf{T})$$

**WHAT(1):** assigns a **transformation index** and the corresponding rotation axis **I + J \***  
**100** or **I \* 1000 + J**

I = index of rotation (**WARNING: NOTE THE SWAP OF VARIABLES**)

J = rotation with respect to axis (1=X, 2=Y, 3=Z)

**WHAT(2):** Polar angle of the rotation ( $0 \leq \vartheta \leq 180^\circ$  degrees)

**WHAT(3):** Azimuthal angle of the rotation ( $-180 \leq \varphi \leq 180^\circ$  degrees)

**WHAT(4), WHAT(5), WHAT(6)** = X, Y, Z offset for the **translation**

**SDUM:** Optional (but recommended) name for the transformation

---

**ROT-DEFI**

Id: 1

Axis: Z ▼

Name: 1tra

Polar: 0.0

Azm:

Δx:

Δy:

Δz: -10.0

# Directives in geometry: warnings

- `$Start_expansion` and `$Start_translat` are applied when reading the geometry → no CPU penalty (the concerned bodies are transformed once for ever at initialization)

`$Start_transform` is applied runtime → some CPU penalty

- One can **nest** the different directives (*at most one per type!*) but, no matter the input order, the adopted sequence is always the following:

`$Start_transform StupiRot`

`$Start_translat -5.0 -7.0 -8.0`

`$Start_expansion 10.0`

`QUA WhatIsIt +1.0 +1.0 +1.0 0.0 0.0 0.0 -10.0 -14.0 -16.0 -2362.0`

`$End_expansion`

`$End_translat`

`$End_transform`

- Directives are not case sensitive (whereas roto-translation names are)

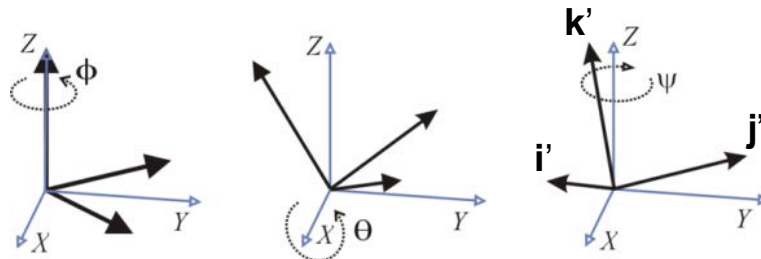


# Identifying rotation angles

Let's define the orientation of a body in the space by a system of 3 orthogonal vectors  $\mathbf{i}'$ ,  $\mathbf{j}'$ ,  $\mathbf{k}'$ , whose coordinates are expressed with respect to the fixed reference frame  $X, Y, Z$

$$\text{Then } [\mathbf{i}' \ \mathbf{j}' \ \mathbf{k}'] = \begin{bmatrix} c_1 c_3 - c_2 s_1 s_3 & -c_1 s_3 - c_3 c_2 s_1 & s_2 s_1 \\ c_2 c_1 s_3 + c_3 s_1 & c_1 c_2 c_3 - s_1 s_3 & -c_1 s_2 \\ s_3 s_2 & c_3 s_2 & c_2 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} \text{ (in the ZXZ convention)}$$

where  $c_1 = \cos(\psi)$   $c_2 = \cos(\theta)$   $c_3 = \cos(\Phi)$   $s_1 = \sin(\psi)$   $s_2 = \sin(\theta)$   $s_3 = \sin(\Phi)$



here  $\Phi = 45^\circ$   $\theta = 30^\circ$   $\psi = -60^\circ$

The obtained Euler angles can be input as azimuthal angle of three consecutive rotations (**ROT-DEFI**)

# Lattice

FLUKA geometry has *replication* (lattice) capabilities

*Only one level is implemented* (no nested lattices are allowed)

- The user defines lattice positions in the geometry and provides transformation rules from the lattice to the prototype region:
  1. in the input with the ROT-DEFI card
  2. in a subroutine (`latic.f`)

The lattice identification is available for scoring

Transformations include:

**Translation, Rotation and Mirroring** (the last only through routine).

# Lattice

- The regions which constitute the **elementary cell** (*prototype*) to be replicated, have to be defined in detail
- The **Lattices** (*replicas/containers*) have to be defined as “empty” regions in their correct location.  
**WARNING:** The lattice region **should map exactly** the outer surface definition of the elementary cell.
- The lattice regions are declared as such with a **LATTICE** card at the end of the geometry input
- In the **LATTICE** card, the user also **assigns lattice names/numbers to the lattices**. These names/numbers will identify the replicas in all FLUKA routines and scoring
- Several basic cells and associated lattices can be defined within the same geometry, one **LATTICE** card will be needed for each set
- **Non-replicas carry the lattice number 0**
- Lattices and plain regions can coexist in the same problem

# LATTICE card

After the Regions definition and before the GEOEND card the user can insert the LATTICE cards

- WHAT(1), WHAT(2), WHAT(3)  
Container region range (from, to, step)
- WHAT(4), WHAT(5), WHAT(6)  
Name/number(s) of the lattice(s)
- SDUM  
 blank to use the transformation from the lattic routine  
 ROT#nn to use a ROT-DEFI rotation/translation from input  
 name the same as above but identifying the roto-translation by the name assigned in the ROT-DEFI SDUM (any alphanumeric string you like)

## Example

```

LATTICE          Reg: TARGR1 ▼      to Reg: ▼      Step:
  Id: 1tra ▼      Lat: 1.0          to Lat: 1.0      Step: 1.0
*...+...1...+...2...+...3...+...4...+...5...+...6...+...7...+...
LATTICE          6.00000  19.00000          101.0000  114.00
  
```

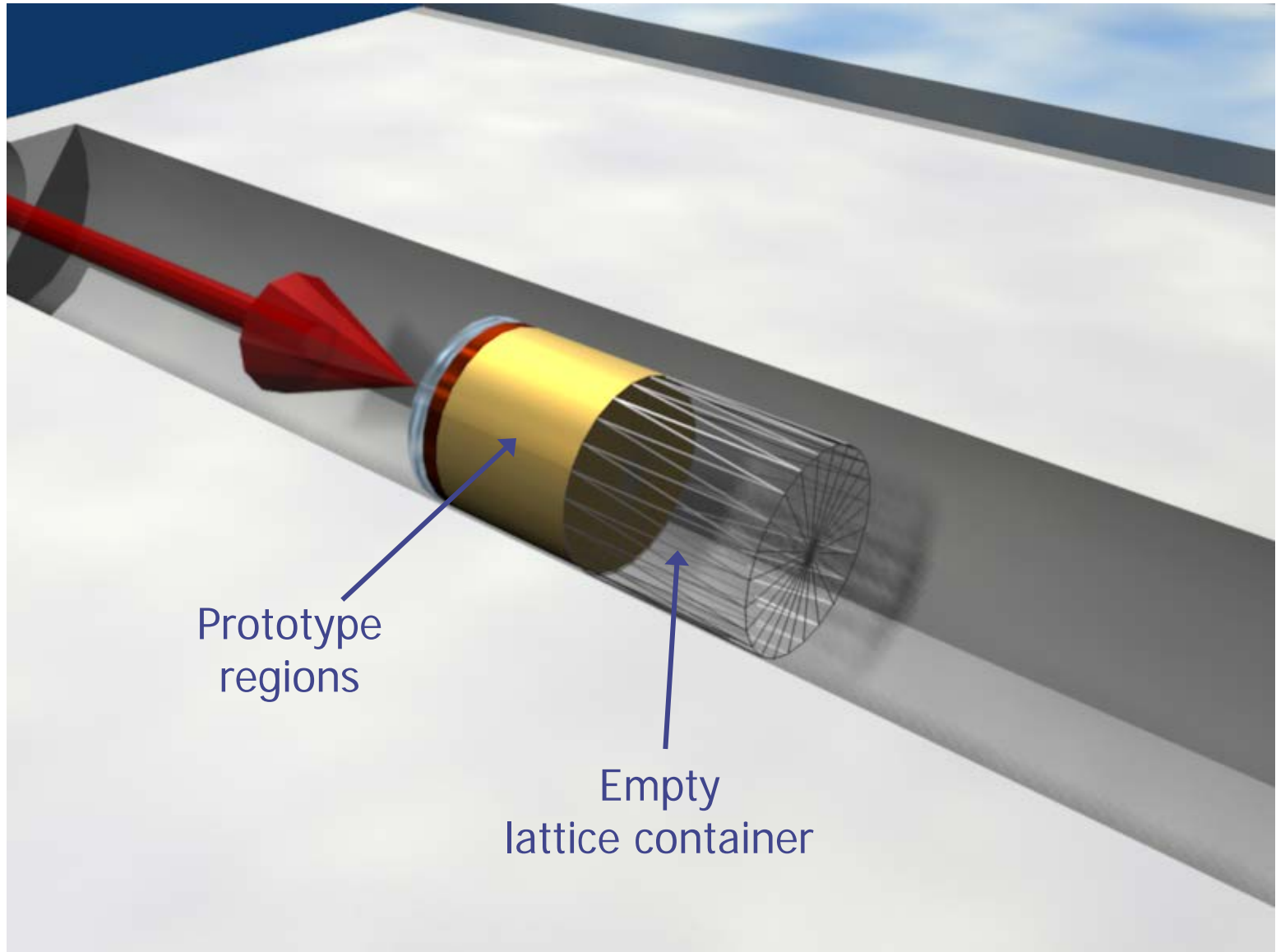
Region # 6 to 19 are the “placeholders” for the first set replicas. We assign to them lattice numbers from 101 to 114

```

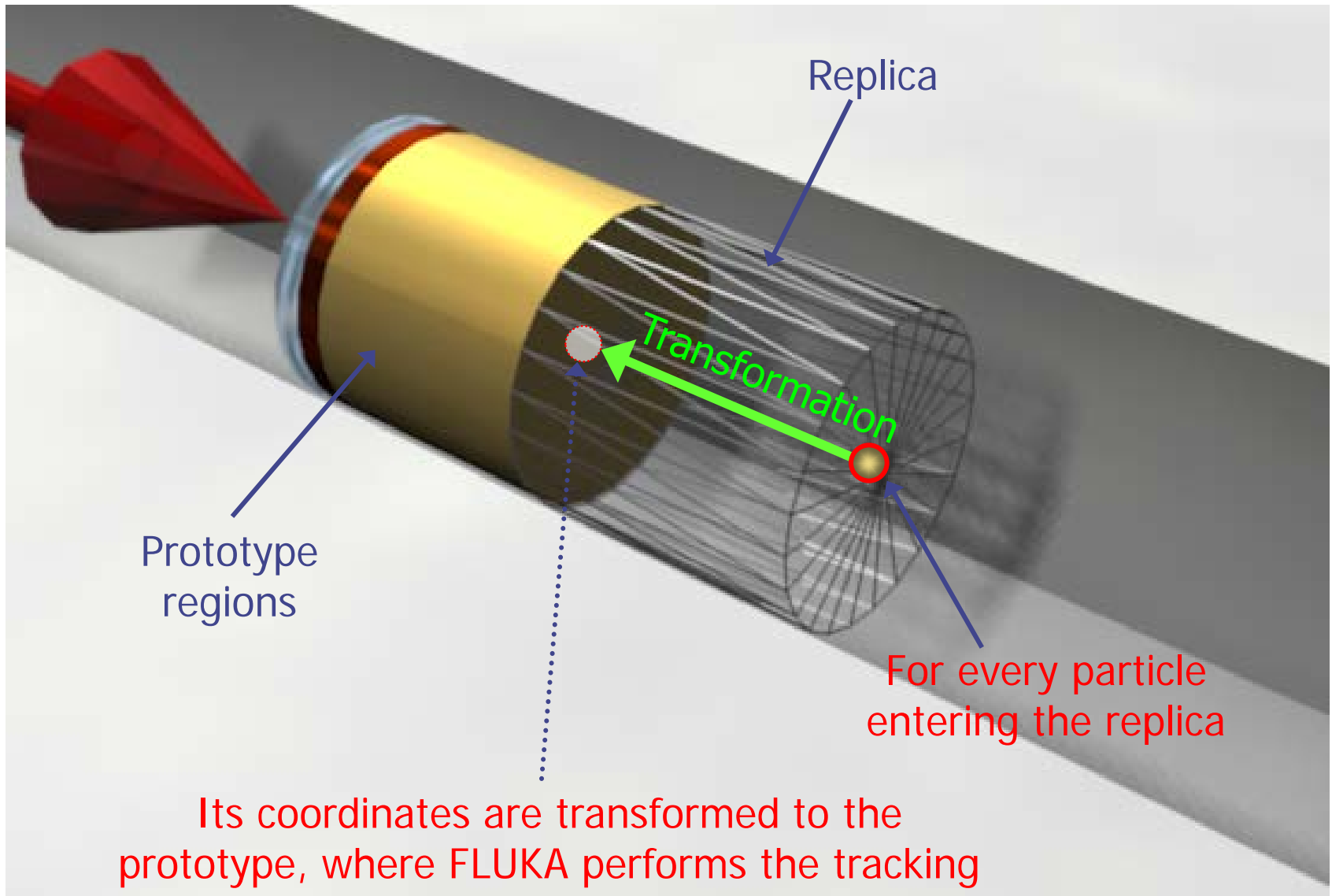
LATTICE          TARGR1          TargRep          1tra
  
```

TARGR1 is the container region using transformation *1tra*

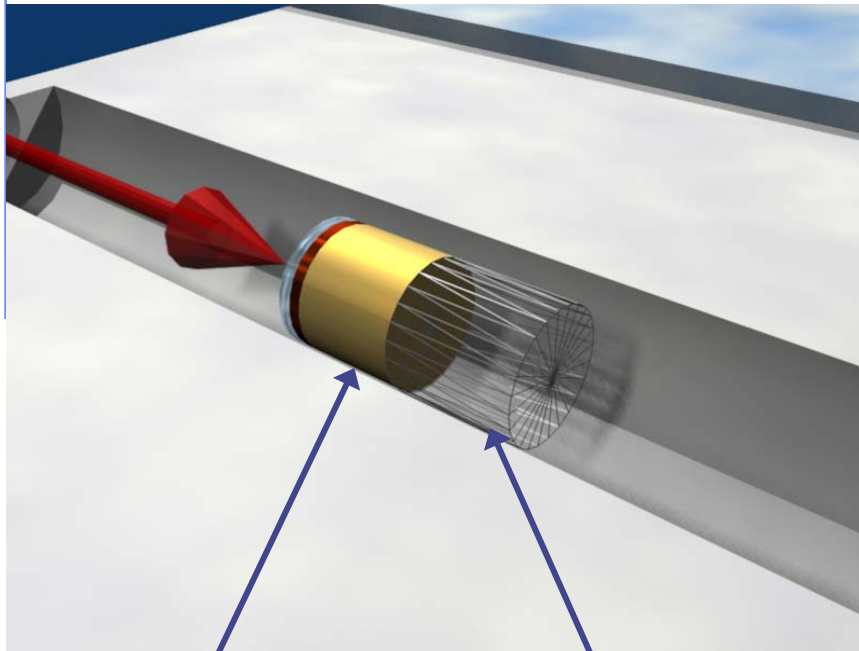
# Example



# Example

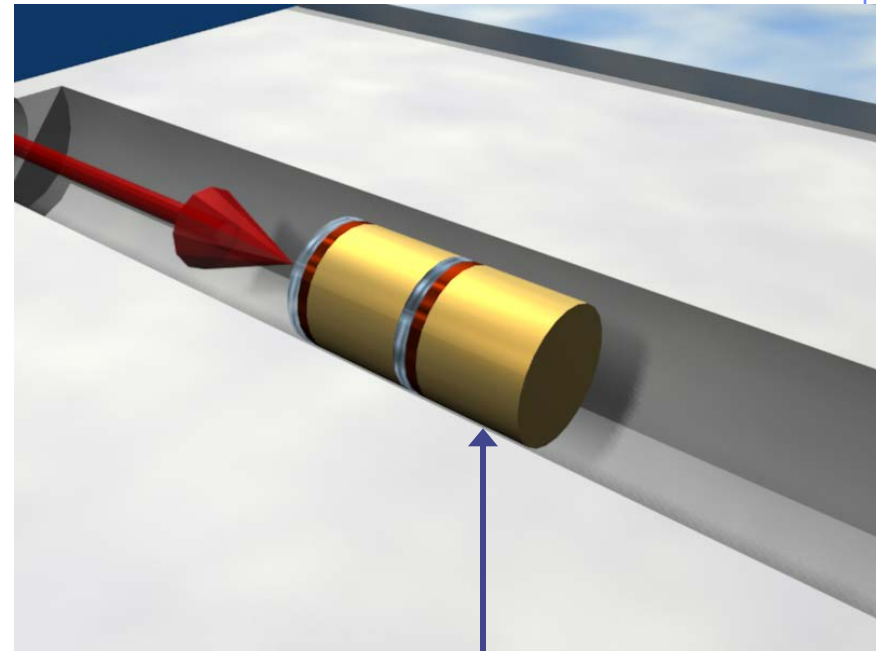


# Example



Prototype  
cell

Empty  
lattice cell



Final  
replica

# Transformation by input

- Rotations/Translations can be defined with the **ROT-DEFIni** card
- Can be assigned to a lattice by **name** or with **ROT#nnn** SDUM in the **LATTICE** card
- **ROT-DEFIni** cards can be consecutive (using the same **index** or **name**) to define complex transformations

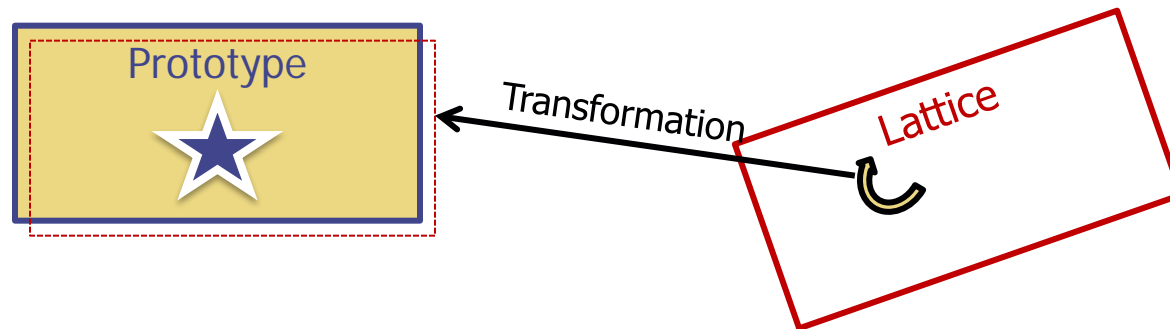
## WARNING:

Since matrix multiplication is not commutative the **order** of the Rotation/Translation operations in 3D is important.



# Numerical Precision


- Due to the nature of the floating point operations in CPU, even if the transformation looks correct the end result could be problematic



This small misalignment between lattice/transformation/prototype could lead to geometry errors

- Use as many digits as possible to describe correctly the prototype and lattice cells as well as the transformation.  
**It is mandatory that the transformation applied to the container makes the latter EXACTLY corresponding to the prototype**
- One can use a **FREE** and **FIXED** card before and after the **ROT-DEFI** to input more than 9 digits
- **GEOBEGIN WHAT(2)** allows to relax the accuracy in boundary identification **(USE WITH CAUTION)**

# Lattice: Important remarks

- Materials and other properties have to be assigned only to the regions constituting the prototype.
- In all (user) routines the **region number** refers to the corresponding one **in the prototype**.
- The **SCORE** summary in the **.out** file and the scoring by regions add together the contributions of the prototype region as well as of all its replicas!
- The lattice identity can be recovered runtime by the *lattice number*, as set in the **LATTICE** card or available through the GEON2L routine if is defined by name 
- In particular, the **LUSRBL** user routine allows to manage the scoring on lattices in the special **USRBIN/EVENTBIN** structure.

# The USRBIN/EVENTBIN special binning

**EVENTBIN** or **USRBIN** with **WHAT(1)=8** :

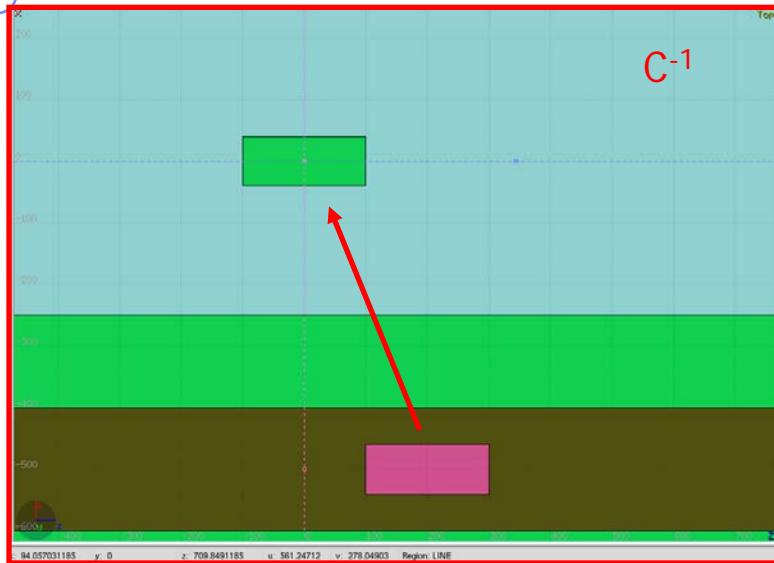
Special user-defined 3D binning. Two variables are discontinuous (e.g. region number), the third one is continuous, but not necessarily a space coordinate.

Variable	Type	Default	Override Routine
1 <sup>st</sup>	integer	region number	MUSRBR
2 <sup>nd</sup>	integer	lattice cell number	LUSRBL
3 <sup>rd</sup>	float	zero	FUSRBV

# Tips & Tricks

- Always remember that the transformation must bring the container onto the prototype and not viceversa!
- You can always divide a transformation into many **ROT-DEFI** cards for easier manipulation.
- Rotations are always around the origin of the geometry, and not the center of the object.
  - To rotate an object, first translate the object to the origin of the axes
  - Perform the rotation
  - Move it by a final translation to the requested position.  
Of course with the inverse order since everything should apply to the replica
- In order to define the replica body, you can clone the body enclosing the prototype (assigning it a new name!) and apply to it the `$Start_transform` directive with the inverse of the respective **ROT-DEFI** transformation.

# Tips & Tricks



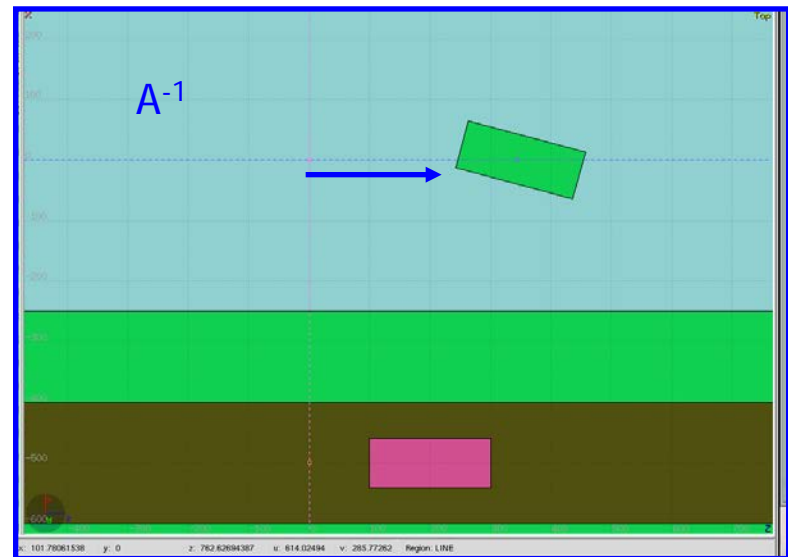
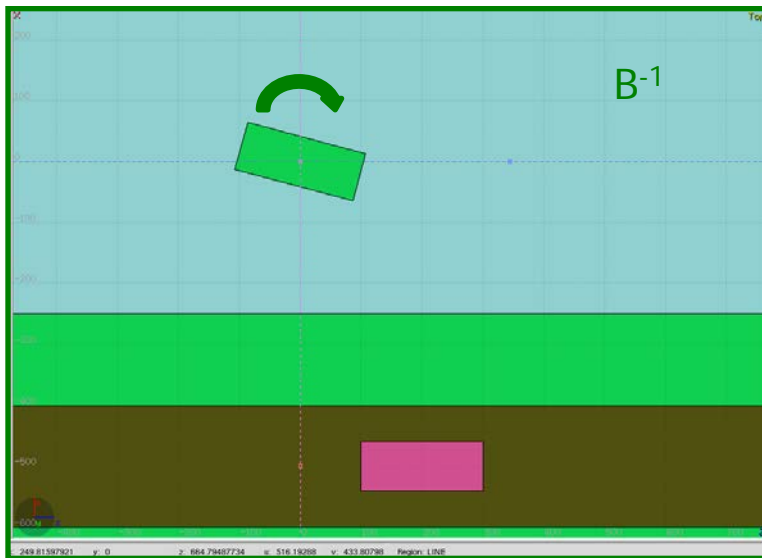
GEOBEGIN

```
...
RPP CollProt -540.0 -460.0 -20.0 20.0 100.0 300.0
$start_transform -rotColl *
RPP CollRepl -540.0 -460.0 -20.0 20.0 100.0 300.0
$end_transform
```

GEOEND

```
ROT-DEFI, 1.0, 0.0, 0.0, 0.0, 0.0, -350.0, rotColl [A]
ROT-DEFI, 201.0, 0.0, -15.0, 0.0, 0.0, 0.0, rotColl [B]
ROT-DEFI, 1.0, 0.0, 0.0, -500.0, 0.0, 200.0, rotColl [C]
```

\* Remember: if  $R=CBA$ , then  $R^{-1}=A^{-1}B^{-1}C^{-1}$

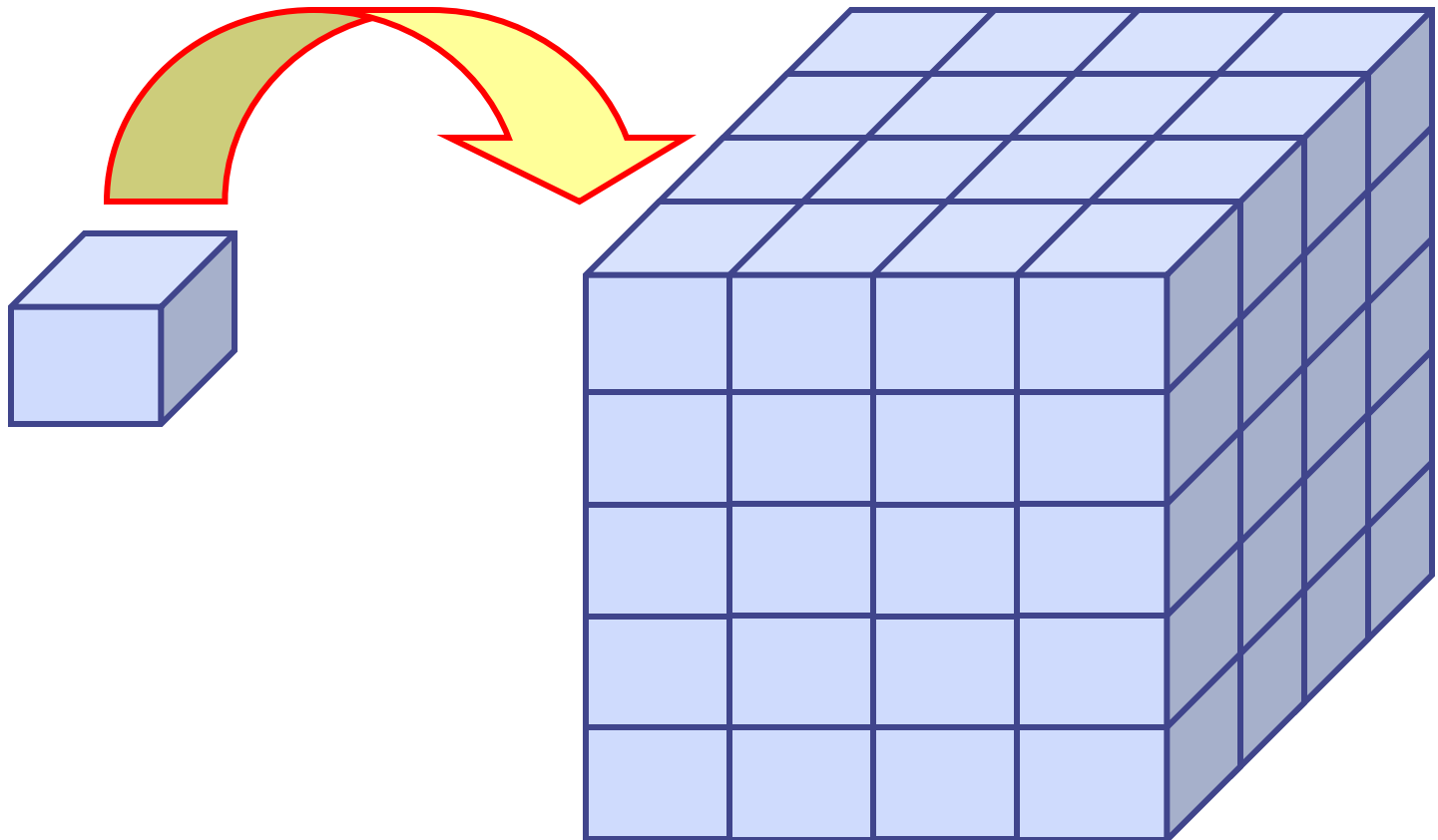


## (Tips & Tricks)

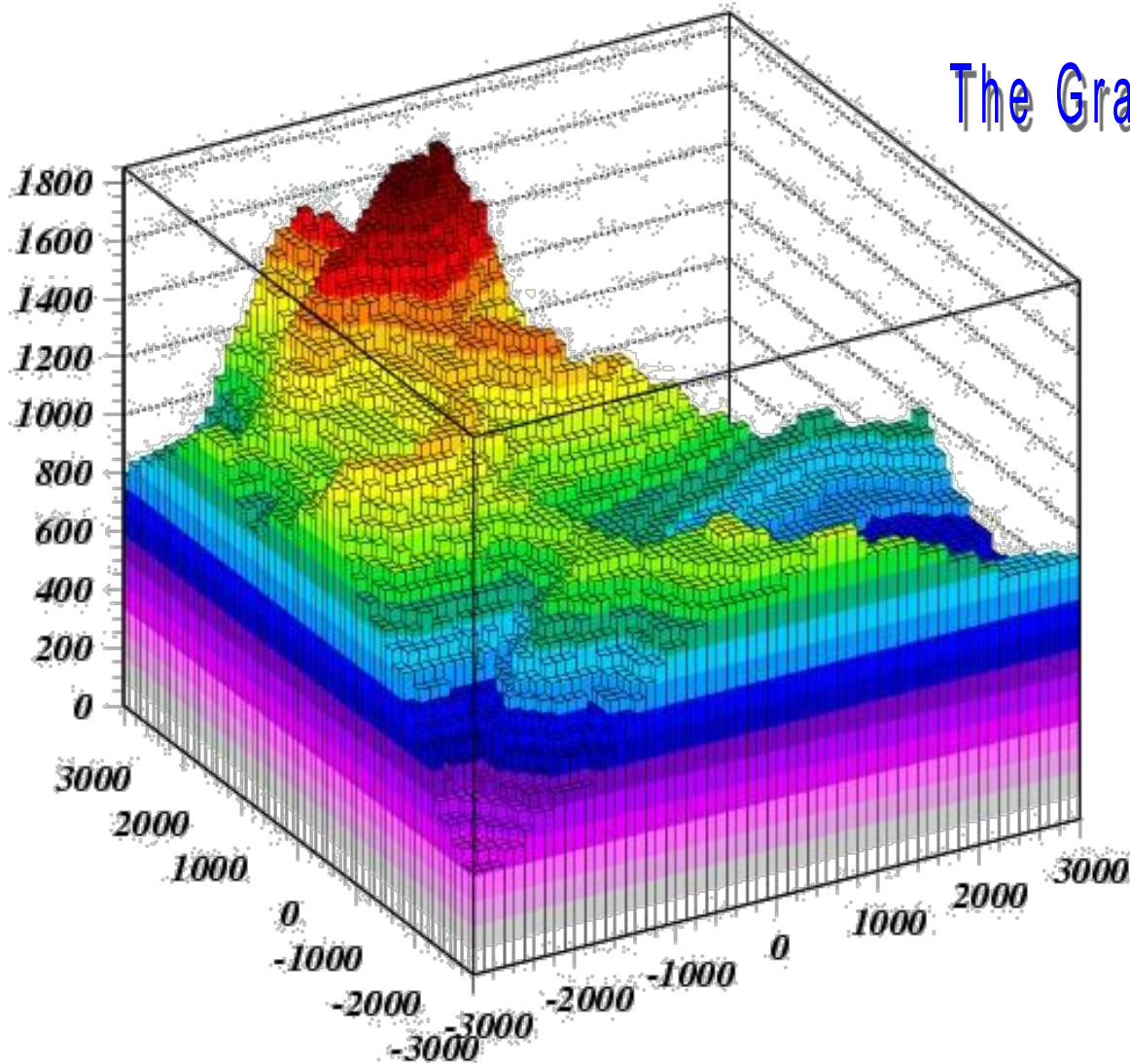
- The **Geometry transformation editor in flair** can read and write **ROT-DEFI** cards with the transformation requested
- An easy way of creating a replica and the associated transformation is the following:
  1. Select the body defining the outer cell of the prototype
  2. Clone it with (**Ctrl-D**) and change the name of the clones. Click on “**No**” when you are prompted to change all references to the original name.
  3. Open the Geometry transformation dialog (**Ctrl-T**)
  4. Enter the transformation of the object in the listbox
  5. Click on “**Transform**” to perform the transformation on the clone bodies
  6. Click on “**Invert**” button to invert the order of the transformation
  7. Enter a name on the “**ROT-DEFIni**” field and click “**Add to Input**” to create the **ROT-DEFIni** cards
  8. Now you have to create manually the needed **regions** and the **LATTICE** cards

# The FLUKA voxel geometry

It is possible to describe a geometry in terms of “**voxels**”, i.e., tiny parallelepipeds (all of equal size) forming a **3-dimensional grid**



# An example



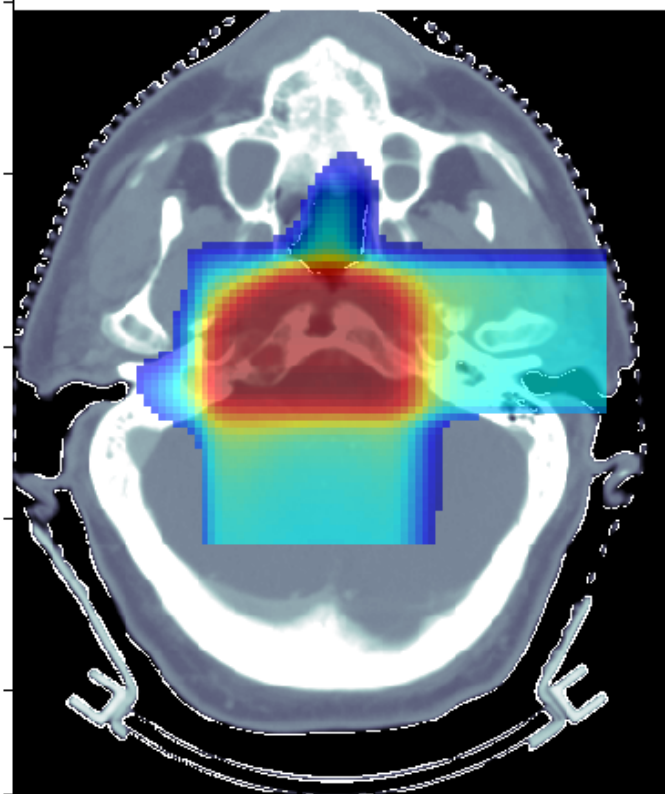
The Gran Sasso in FLUKA



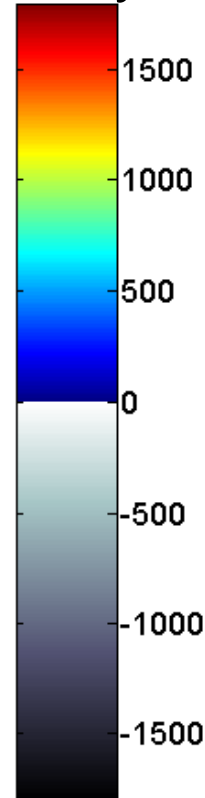
# Another example, for medical applications

Voxel geometries are especially useful to import CT scan of a human body, e.g., for dosimetric calculations of the planned treatment in radiotherapy

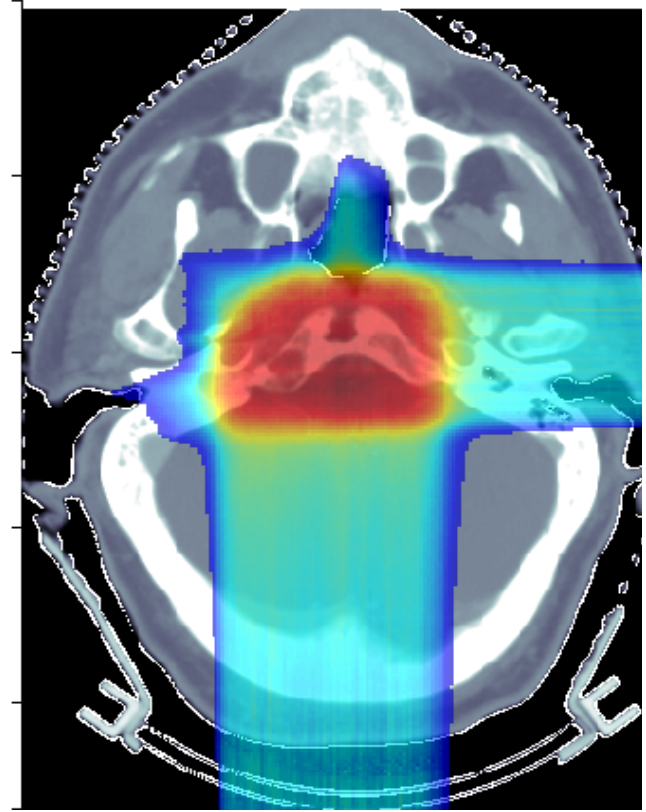
**Commercial TPS**



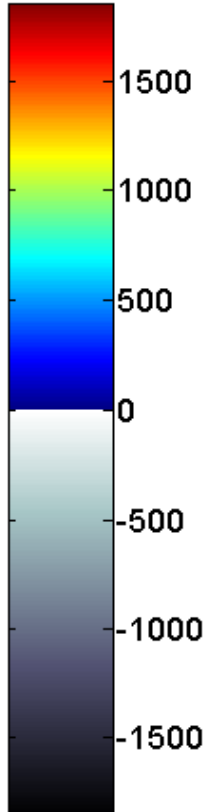
mGy



**FLUKA**



mGy



# Concepts

- The CT scan contains integer values “Hounsfield Unit” reflecting the X-ray attenuation coefficient  $\mu_x$

$$HU_x = 1000 (\mu_x - \mu_{H2O}) / \mu_{H2O}, \text{ typically } -1000 \leq HU \leq 3500$$

- We will use loosely the word “**organ**” to indicate a **group of voxels** (or even more than one group) **made of the same “tissue” material** (same HU value or in a given HU interval)
- The code handles each **organ** as a **CG region**, possibly in addition to other conventional “**non-voxel**” regions defined by the user
- The voxel structure can be complemented by parts written in the standard Combinatorial geometry
- The code assumes that the voxel structure is contained in a parallelepiped. This RPP is automatically generated from the voxel information.

# Procedure

- To describe a voxel geometry, the user must convert his CT scan or equivalent data to a format understood by FLUKA
- This stage should :
  - Assign an **organ index** to **each voxel**. In many practical cases, the user will have a **continuum of CT values (HU)**, and may have to **group these values in intervals**
  - Each **organ** is identified by a **unique integer  $\leq 32767$** . The organ numbering **does not need to be contiguous** (i.e. “holes” in the numbering sequence are allowed.)
  - **One of the organs** must have number **0** and plays the role of the **medium surrounding the voxels** (usually vacuum or air).
  - The user assigns to **each NONZERO organ** a **voxel-region number**. The voxel-region numbering has to be **contiguous** and starts **from 1**.

# Procedure

- The information is input to FLUKA through a special **unformatted** file \*vxl containing:
  - The number of voxels along each coordinate axis
  - The number of voxel-regions, and the maximum organ number
  - The voxel dimension along each coordinate axis
  - A 3D matrix specifying the organ to which each voxel corresponds in Fortran list-oriented format, with the x coordinate running faster than y, and y running faster than z.

val(1)	corresponds to 1,1,1 == organ # of first voxel
...	...
val(N <sub>x</sub> )	corresponds to N <sub>x</sub> ,1,1
val(N <sub>x</sub> +1)	corresponds to 1,2,1
...	...
val(2*N <sub>x</sub> )	corresponds to N <sub>x</sub> ,2,1
...	...
val(N <sub>y</sub> *N <sub>x</sub> )	corresponds to N <sub>x</sub> ,N <sub>y</sub> ,1
...	...
val(N <sub>z</sub> *N <sub>y</sub> *N <sub>x</sub> )	corresponds to N <sub>x</sub> ,N <sub>y</sub> ,N <sub>z</sub> == organ # of last voxel

- A list of the voxel-region number corresponding to each organ

# Input file: geometry description

Prepare the usual FLUKA input file.

The geometry is written like a normal Combinatorial Geometry input, but in addition a **VOXELS** card must be inserted right after the GEOBEGIN card and before the Geometry title card

- **WHAT(1), WHAT(2), WHAT(3)** = x, y, z coordinates chosen as the origin of the “**voxel volume**”, i.e. the corner of a RPP extending from **WHAT(1)** to **WHAT(1) + NX\*DX**, ... and containing all the voxels
- **WHAT(4)** possible ROT-DEFI **transformation applying to the RPP**
- (**WHAT(5), WHAT(6)**): not used)
- **SDUM** = name of the voxel file  
(extension will be assumed to be **.vxl**)

```
VOXELS    -20.0    -30.0    -40.0  transf                ct
```

# Input file: geometry description

One will have

- The usual list of **NB bodies**, not including the **RPP** corresponding to the “**voxel volume**” (see **VOXELS** card above). This **RPP** will be generated and added automatically by the code as the  $(\mathbf{NB}+1)^{\text{th}}$  body, with one corner in the point indicated in the **VOXELS** card, and dimensions **NX\*DX**, **NY\*DY** and **NZ\*DZ** as read from the voxel file.
- The usual list of **NR regions**, with the space occupied by the body named **VOXEL** or numbered **NB+1** (the “**voxel volume**”) subtracted. In other words, the **NR** listed regions must cover the whole available space, except the space corresponding to the “**voxel volume**”. This is easily obtained by subtracting the body **VOXEL** (or **NB+1**) in the relevant region definitions, even though this body is not explicitly input at the end of the body list.

\* vacuum inside

```
VACI      5 +SHI +SHTB -SHBT -VOXEL
```

# Voxel Regions

The code will automatically generate  $NO+2$  additional regions, where  $NO$  = number of non-zero organs:

Name	Number	Description
VOXEL	NR+1	sort of a “cage” for all voxels. Nothing should ever be deposited in it. The user shall assign VACUUM to it.
VOXEL001	NR+2	containing all voxels belonging to organ number 0. There must be at least 2 of such voxels, but in general they should be many more. Typical material assignment to this region is air
VOXEL002	NR+3	corresponding to organ 1
VOXEL003	NR+4	corresponding to organ 2
VOXEL###	NR+2+NO	corresponding to organ NO

# Voxel Material Assignment

The assignment of materials shall be made by the card **ASSIGNMA**t (and in a similar way for other region-dependent options) referring to the first **NR** regions in the usual way, and to the additional voxel regions using the correspondence to organs.

	ASSIGNMA	BLCKHOLE	BLKH
	ASSIGNMA	VACUUM	VACO
	ASSIGNMA	ALUMINUM	AL
	ASSIGNMA	VACUUM	VACI
cage	ASSIGNMA	VACUUM	VOXEL
0 Organ	ASSIGNMA	VACUUM	VOXEL001
6 "Non-zero" organs	ASSIGNMA	TITANIUM	VOXEL002
	ASSIGNMA	AIR	VOXEL003
	ASSIGNMA	COPPER	VOXEL004
	ASSIGNMA	CALCIUM	VOXEL005
	ASSIGNMA	CARBON	VOXEL006
	ASSIGNMA	AIR	VOXEL007



# Summary of the relevant input cards

\$Start\_expansion      \$End\_expansion  
\$Start\_translat      \$End\_translat      (inside the geometry input)  
\$Start\_transform      \$End\_transform  
to manipulate bodies

## ROT-DEFI

to define roto-translations

## LATTICE (inside the geometry input)

to declare a region as a replica placeholder and associate it to a given transformation

## VOXEL (inside the geometry input)

to introduce a voxel geometry