



# Heavy Ions Interactions

FLUKA Beginner's Course

# Overview

## The models

DPMJET  
RQMD  
BME

## Input options

Beam definition  
Transport thresholds

# Heavy ion interaction models in FLUKA - 1

$E > 5 \text{ GeV/n}$

Dual Parton Model (DPM)

DPMJET-III (original code by R.Engel, J.Ranft and S.Roesler,  
FLUKA-implemenation by T.Empl *et al.*)

$\sim 0.1 \text{ GeV/n} < E < 5 \text{ GeV/n}$

Relativistic Quantum Molecular Dynamics Model (RQMD)

RQMD-2.4 (original code by H.Sorge *et al.*,  
FLUKA-implementation by A.Ferrari *et al.*)

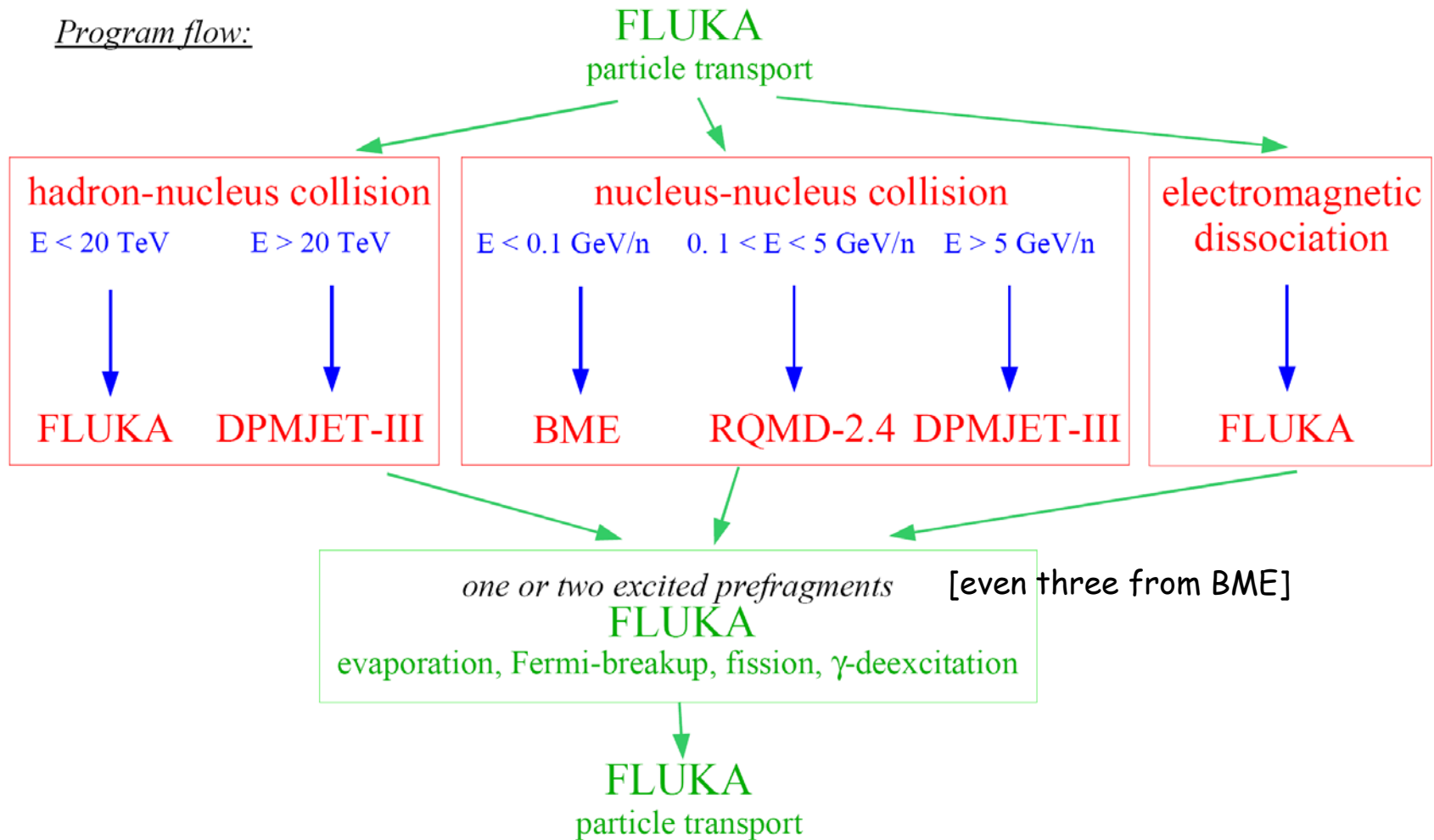
$E < \sim 0.1 \text{ GeV/n}$

Boltzmann Master Equation (BME) theory

BME (original code by E.Gadioli *et al.*,  
FLUKA-implementation by F.Cerutti *et al.*)

# Heavy ion interaction models in FLUKA - 2

*Program flow:*



# DPMJET

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## DPMJET - *Overview*

DPMJET = Dual Parton Model and JETs

Monte Carlo **event-generator** for the simulation of high-energy hadronic interactions

- hadron-hadron collisions,  
hadron-nucleus collisions,  
nucleus-nucleus collisions,  
photoproduction off nuclei (only Version III)
- energy range: 5 GeV/nucleon –  $10^{11}$  GeV/nucleon
- programming language: Fortran77
- size of the code (Version III): about 90.000 lines
- authors: J. Ranft (Version II),  
R.Engel, J. Ranft, S. Roesler (Version III)

# DPMJET - Main steps of a high energy interaction

## 1. Interaction of high-energy nuclei

- individual nucleon-nucleon scatterings
- formation of »strings« between valence and sea partons (quarks, gluons)



## 2. Hadronization process

- creation of hadrons / resonances



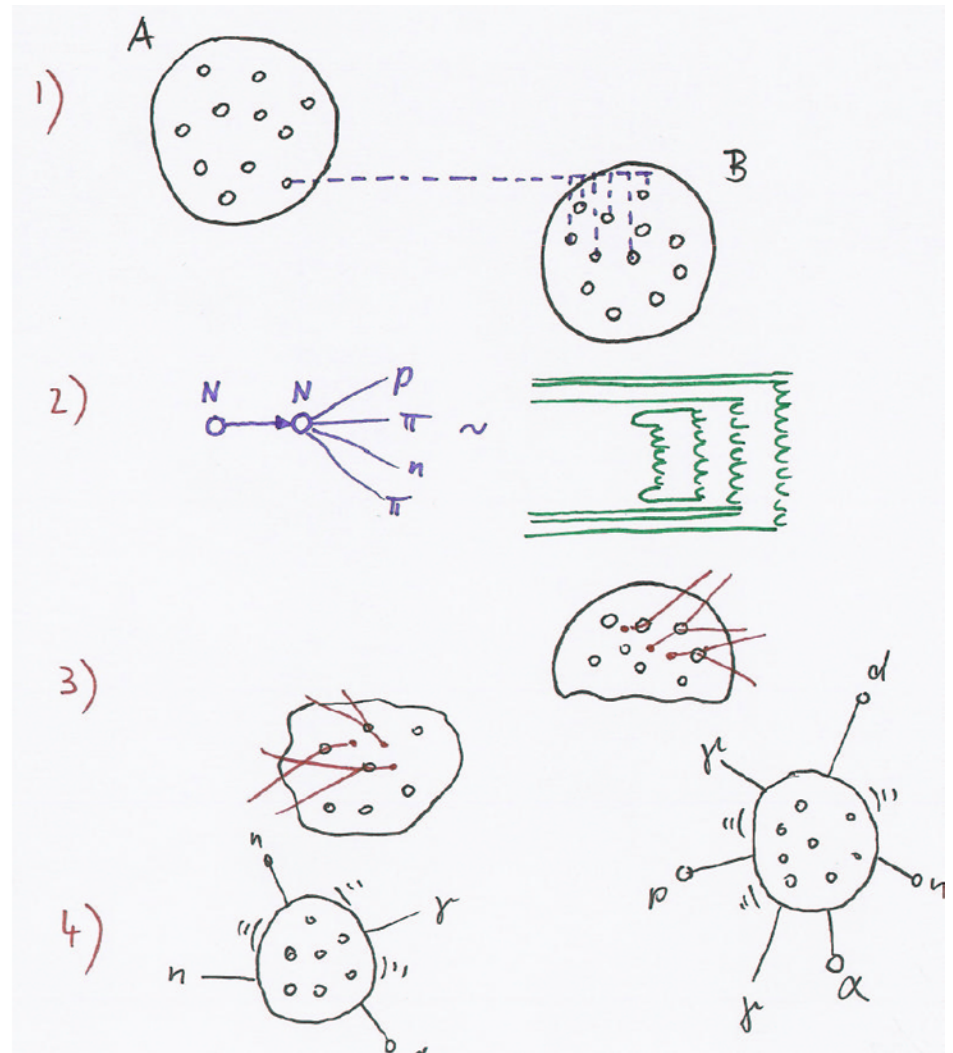
## 3. Intranuclear cascade

- low-energy interactions of hadrons in spectator nuclei



## 4. Fragmentation of excited spectator nuclei

- evaporation of light fragments (e.g., p, n, d,  $^3\text{H}$ ,  $^3\text{He}$ ,  $^4\text{He}$ ,...),
- fragmentation, fission
- production of residual nuclei



# DPMJET - *The Gribov-Glauber formalism*

*Fundamental idea:* nucleus-nucleus collision expressed in terms of individual nucleon-nucleon interactions

- nucleus-nucleus

- total cross section

$$\sigma_{AB}^{tot}(s) = 4 \int d^2 \vec{B} \mathfrak{I} [A_{AB}(s, \vec{B})]$$

- elastic cross section

$$\sigma_{AB}^{el}(s) = 4 \int d^2 \vec{B} \left| A_{AB}(s, \vec{B}) \right|^2$$

- scattering amplitude

$$A_{AB} = \frac{i}{2} \left[ 1 - \exp(\chi_{AB}) \right]$$

eikonal function

$$\chi_{AB} = \sum_{k,l} \chi_{N_k N_l}$$

- nucleon-nucleon

- scattering amplitude

$$a_{N_k N_l} = \frac{i}{2} \left[ 1 - \exp(\chi_{N_k N_l}) \right]$$



## DPMJET - *Intranuclear cascade and fragmentation*

- nuclear model :
  - Fermi-gas of nucleons in potential well
  - nuclear densities: shell model ( $A \leq 18$ )  
Wood-Saxon ( $A > 18$ )
- hadrons are followed in space and time on straight trajectories
- hadrons may re-interact after certain formation-time  
(assume local nuclear density and vacuum cross sections)
- calculation of excitation energies (in AA interactions for both spectators)

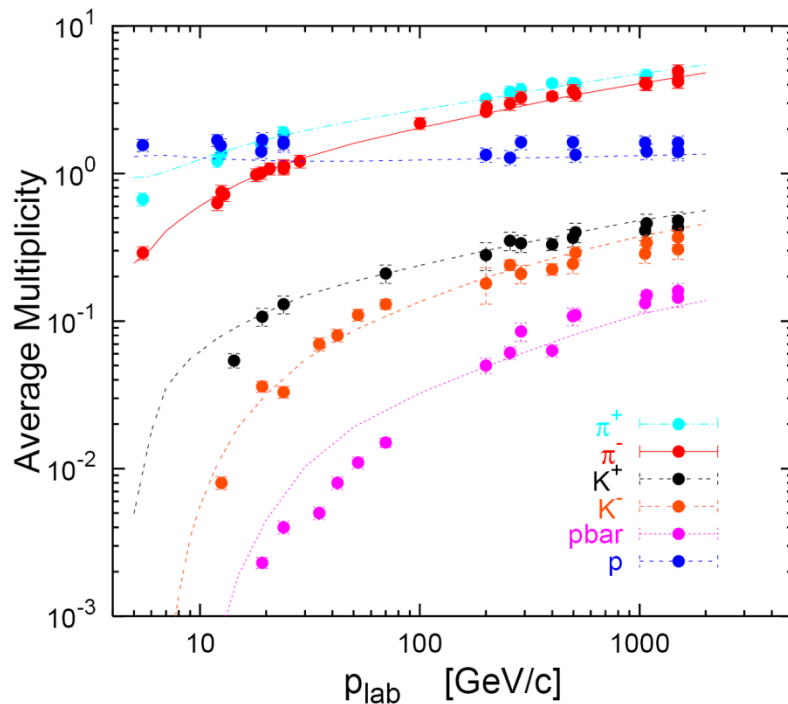
*Note: DPMJET has its own implementation of intranuclear cascades. It is similar in its fundamental ideas to that one of FLUKA but is much more simplified.*

- fragmentation by
    - nuclear evaporation
    - Fermi-breakup
    - high-energy fission
    - $\gamma$ -deexcitation
- } FLUKA

# DPMJET - Comparison to data (hadron-hadron)

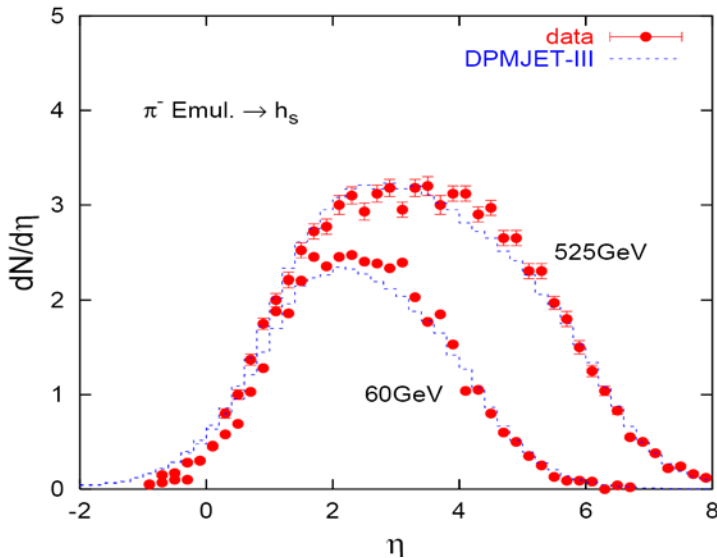
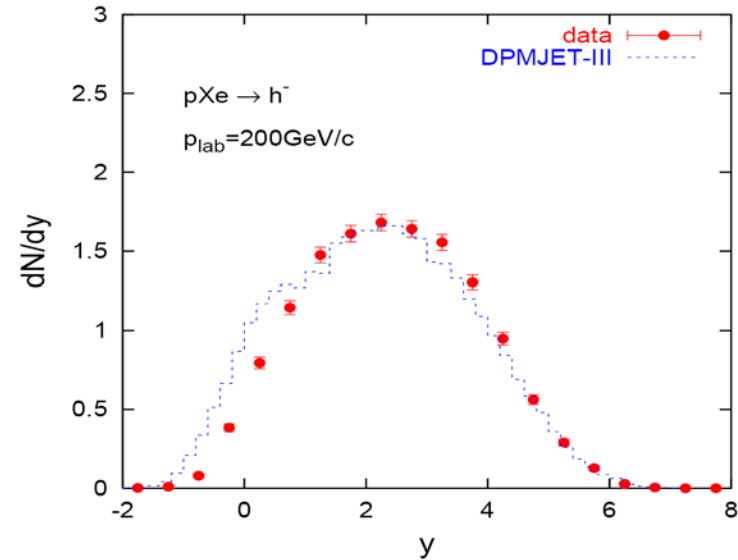
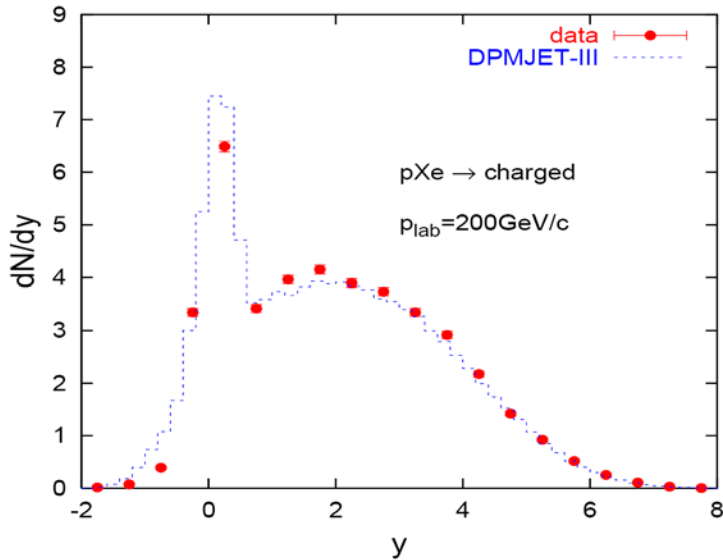
proton - proton

proton - proton,  $E_{\text{lab}} = 200\text{GeV}$



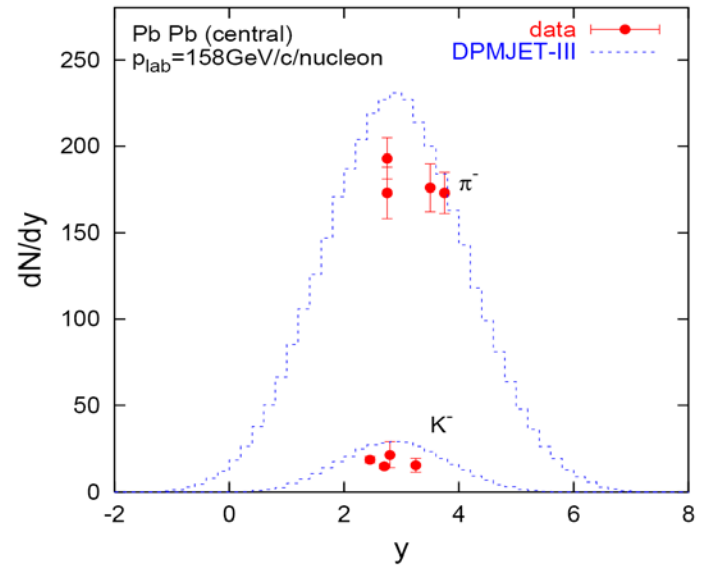
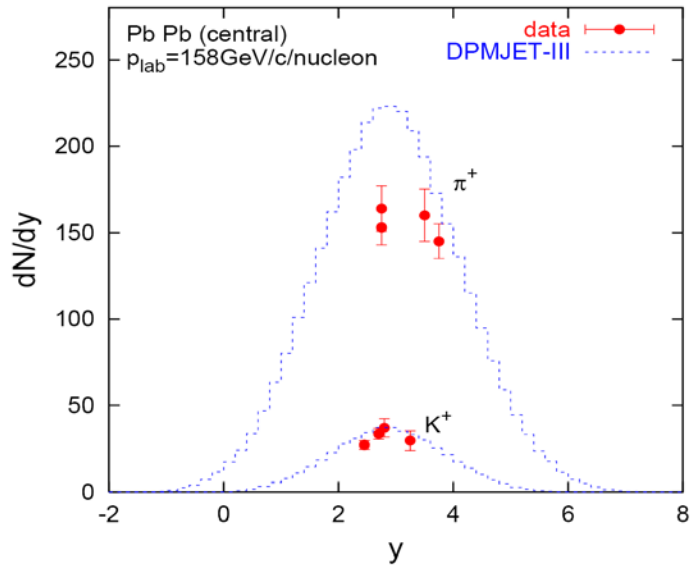
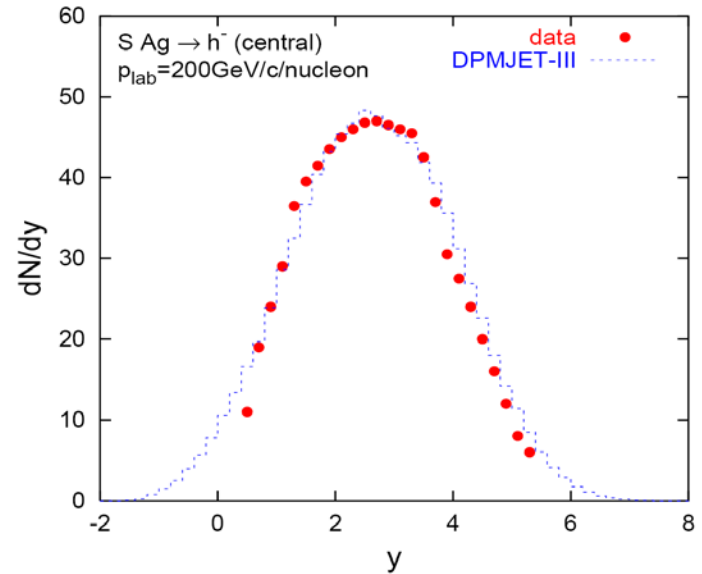
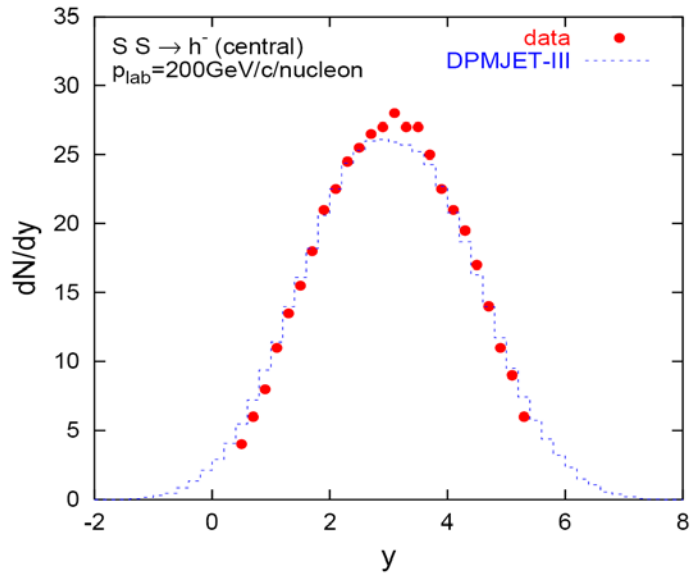
	Exp.	DPMJET-III
charged	$7.69 \pm 0.06$	7.64
neg.	$2.85 \pm 0.03$	2.82
p	$1.34 \pm 0.15$	1.26
n	$0.61 \pm 0.30$	0.66
$\pi^+$	$3.22 \pm 0.12$	3.20
$\pi^-$	$2.62 \pm 0.06$	2.55
$K^+$	$0.28 \pm 0.06$	0.30
$K^-$	$0.18 \pm 0.05$	0.20
$\Lambda$	$0.096 \pm 0.01$	0.10
$\bar{\Lambda}$	$0.0136 \pm 0.004$	0.0105

# DPMJET - Comparison to data (hadron-nucleus)

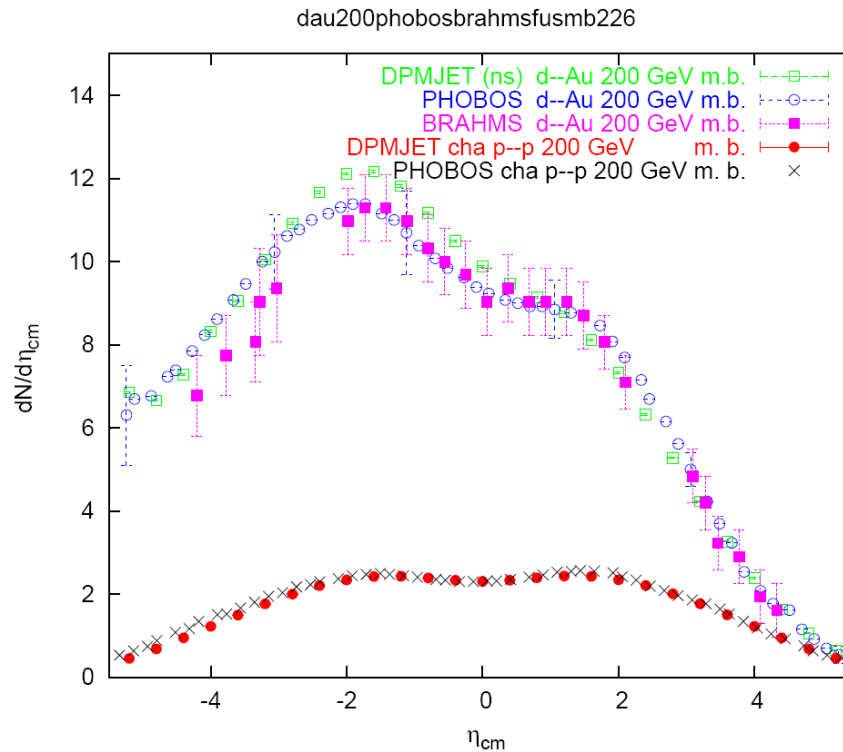


	Exp.	DPMJET-III
14.6 GeV p Al	$1.57 \pm 0.23$	1.52
p Au	$2.15 \pm 0.33$	1.92
200 GeV p S	$5.0 \pm 0.2$	4.98
p Xe	$6.84 \pm 0.13$	6.67
360 GeV p Al	$6.8 \pm 0.6$	5.87
p Au	$8.9 \pm 0.4$	8.77

# DPMJET - Comparison to data (nucleus-nucleus)



# DPMJET - Comparison to data (nucleus-nucleus)

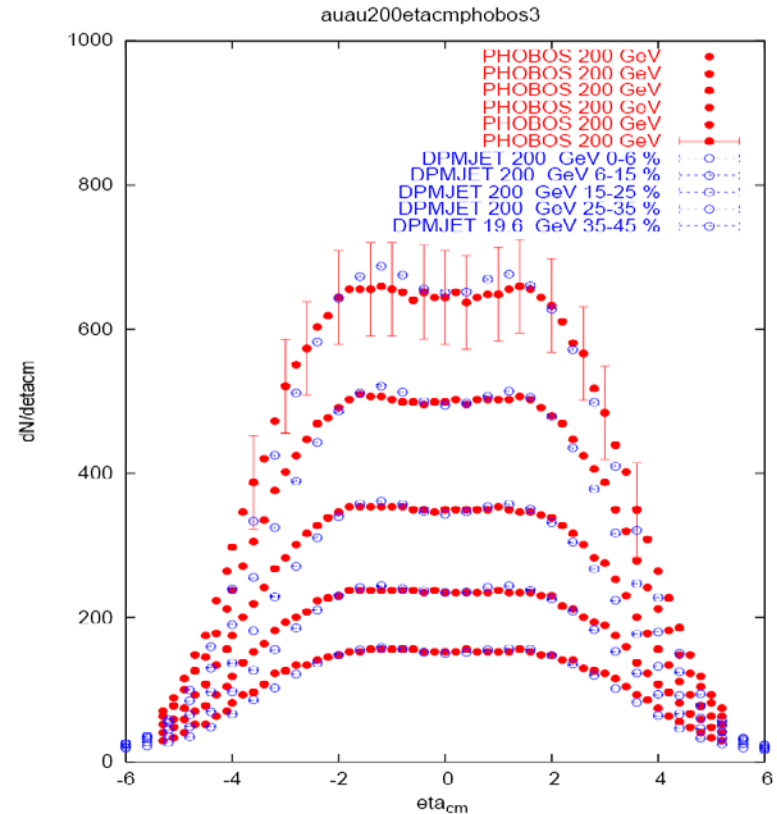
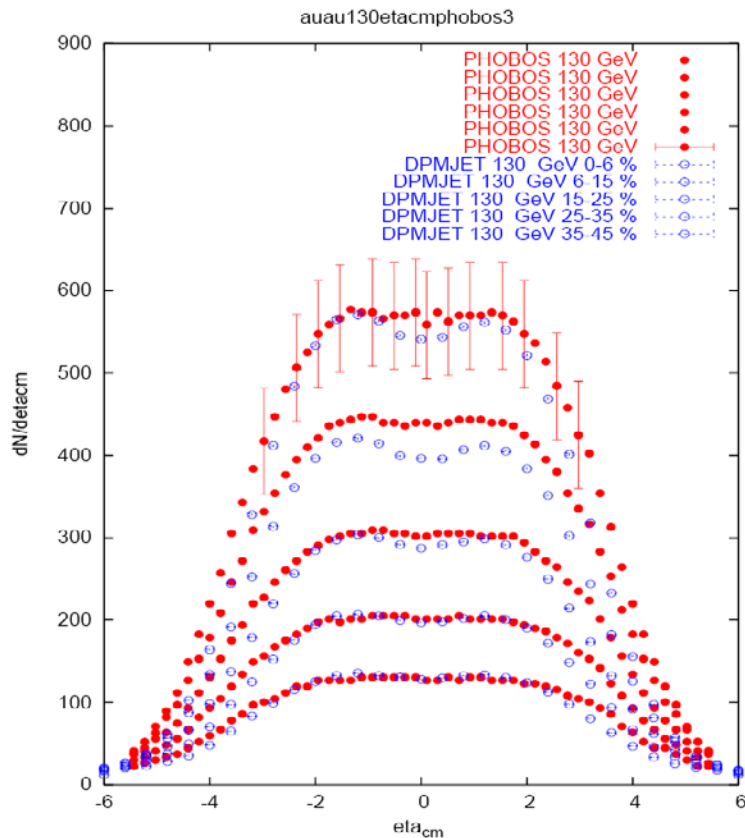


Pseudorapidity distribution of charged hadrons produced in minimum bias d-Au and p-p collisions at a c.m. energy of 200GeV/A.

Exp. data: BRAHMS- and PHOBOS-Collaborations

J.Ranft, in Proceedings of the Hadronic Shower Simulation Workshop, CP896, Batavia, Illinois (USA), 6-8 September 2006

# DPMJET - Comparison to data (nucleus-nucleus)

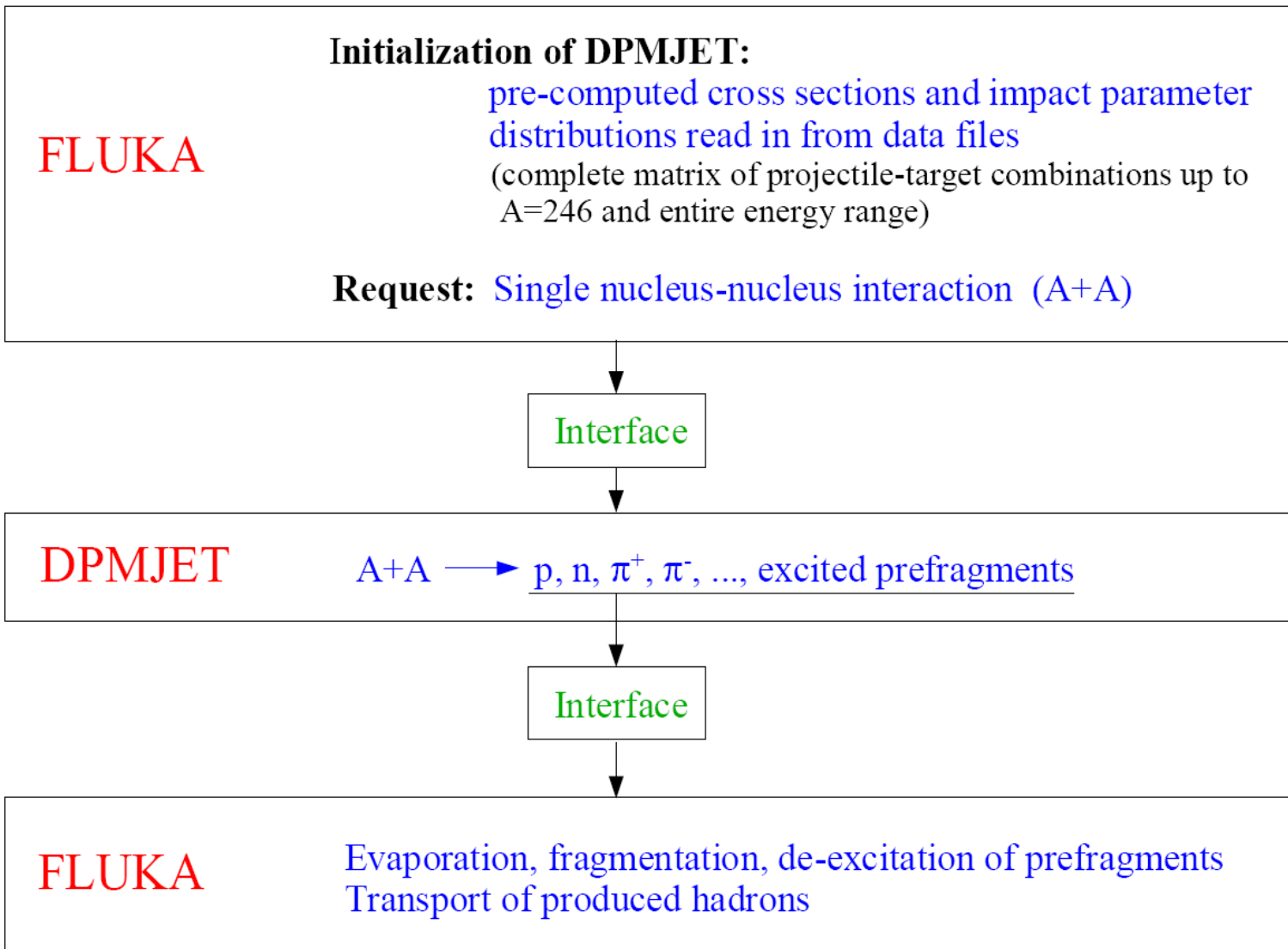


Pseudorapidity distribution of charged hadrons produced in Au-Au collisions at a c.m. energy of 130 GeV/A (left) and 200 GeV/A (right) for different ranges of centralities.

Exp. data: PHOBOS-Collaboration

J.Ranft, in Proceedings of the Hadronic Shower Simulation Workshop, CP896, Batavia, Illinois (USA), 6-8 September 2006

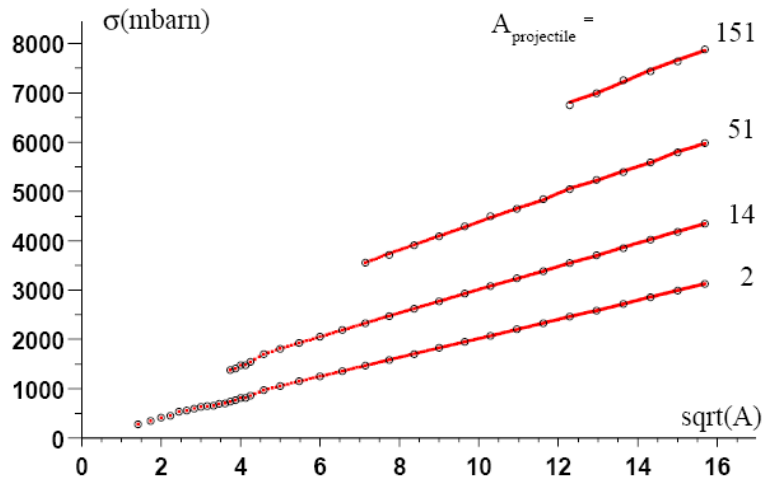
# DPMJET - Interface to FLUKA



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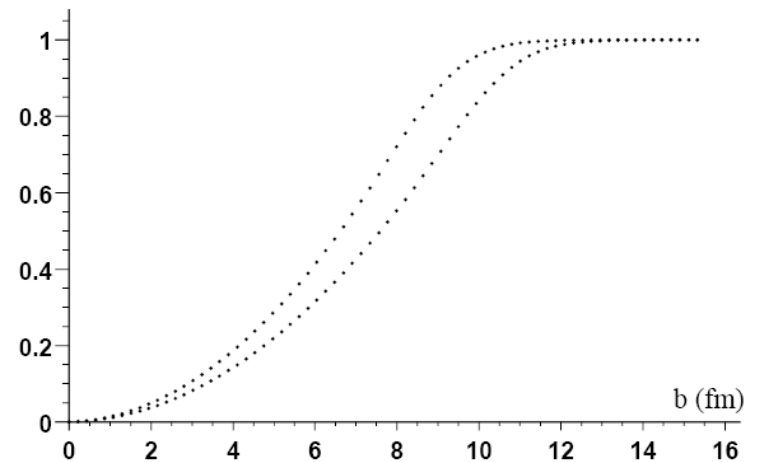
## Examples for pre-initialised data:

### Inelastic cross sections



$$E_{\text{Lab}} = 6.3 \times 10^9 \text{ GeV/nucleon}$$

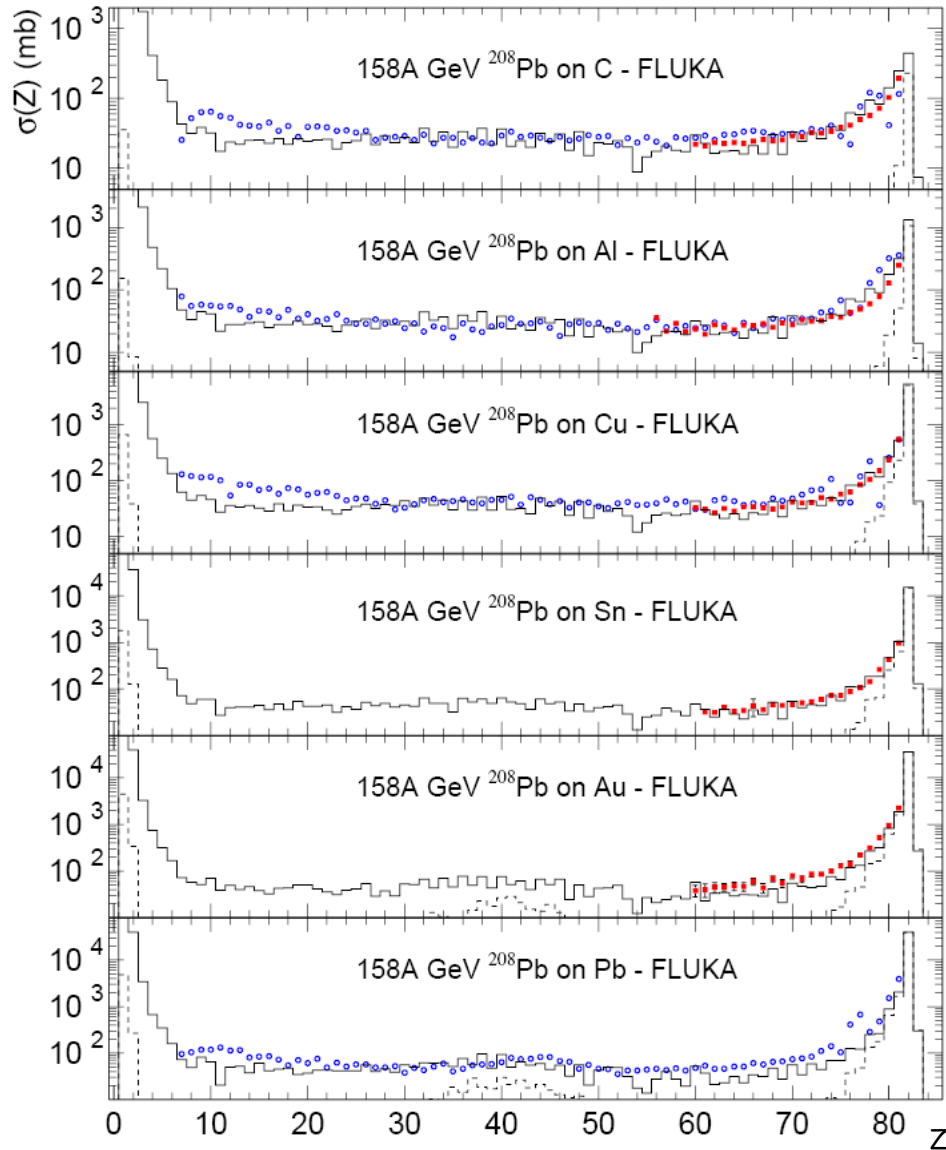
### Impact parameter distribution



e.g., for highest and lowest energy at one fixed projectile-target configuration



# DPMJET - FLUKA benchmarks



Fragment charge cross sections for  
158GeV/n Pb ions on various targets.  
FLUKA: solid histogram (total)  
dashed histogram (em diss.)  
Exp. data: symbols  
NPA662, 207 (2000),  
NPA707, 513 (2002),  
C.Scheidenberger *et al.* PRC

# RQMD

$E > 5 \text{ GeV/n}$

Dual Parton Model (DPM)  
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$E < 0.1 \text{ GeV/n}$

Boltzmann Master Equation (BME) theory  
BME (original code by E.Gadioli *et al.*,  
FLUKA-implementation by F.Cerutti *et al.*)

## RQMD - *References*

interface to a suitably modified **RQMD model**

RQMD-2.4 (H. Sorge, 1998) was successfully applied  
to relativistic A-A particle production over a wide energy range

[H. Sorge, Phys. Rev. **C 52**, 3291 (1995);

H. Sorge, H. Stöcker, and W. Greiner, Ann. Phys. **192**, 266 (1989)

and Nucl. Phys. **A 498**, 567c (1989)]

# RQMD - *The original code*

## The RQMD-2.4 code

**INITIAL CONDITION** two Fermi gases (projectile and target)

$$\text{Fermi momentum } p_{F0} = \hbar \left( 3\pi^2 \frac{A}{2V} \right)^{1/3} \quad V = (4/3) \pi (r_0 A^{1/3})^3 \quad r_0 = 1.12 \text{ fm} \Rightarrow \rho = 0.17 \frac{\text{nucl.}}{\text{fm}^3}$$

$$\text{nucleon momentum } \boxed{p = p_{F0} \left( \frac{\rho(r)}{\rho_0} \right)^{1/3} \epsilon^{1/3}} \quad \epsilon \in [0, 1] \text{ random}$$
$$\phi = 2\pi\epsilon \qquad \cos \theta = 1 - 2\epsilon$$

$$p_x = p \sin \theta \cos \phi \quad - (\sum p_x) / A$$

$$p_y = p \sin \theta \sin \phi \quad - (\sum p_y) / A$$

$$p_z = p \cos \theta \quad - (\sum p_z) / A$$

$$\text{so } \sum p_x = \sum p_y = \sum p_z = 0$$

## FINAL STATE

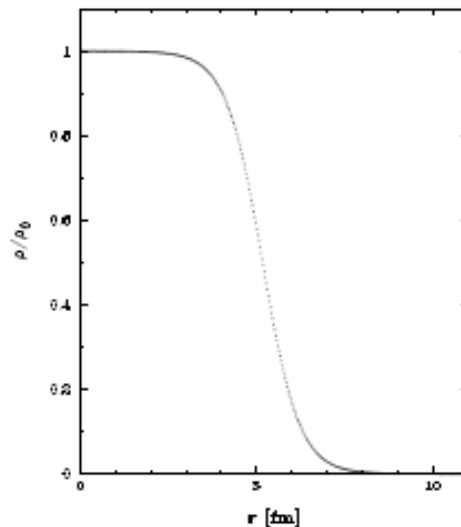
- $(p^0, p_x, p_y, p_z)$  for nucleons (and produced particles) in the LAB frame
- the spectators are marked
- no residue and fragment identification
- energy non-conservation issues, particularly when run in full QMD mode

# RQMD - *The interfaced code*

## Implemented developments

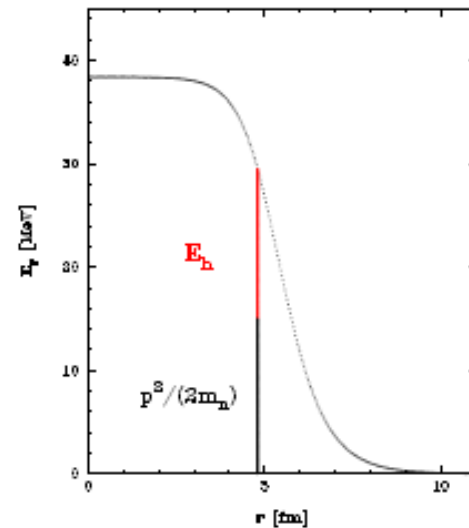
- construct the **projectile- and target-like** nuclei by gathering *spectator* nucleons,

$$\text{assuming } E_{PL}^* = \sum_{pa.} \rho E_h \quad (TL)$$



$$\rho(r) \propto \left(1 + \exp\left(\frac{r-R}{a}\right)\right)^{-1}$$

$$R = 1.19 A^{1/3} - 1.61 A^{-1/3} \text{ fm} \quad a = 0.52 \text{ fm}$$

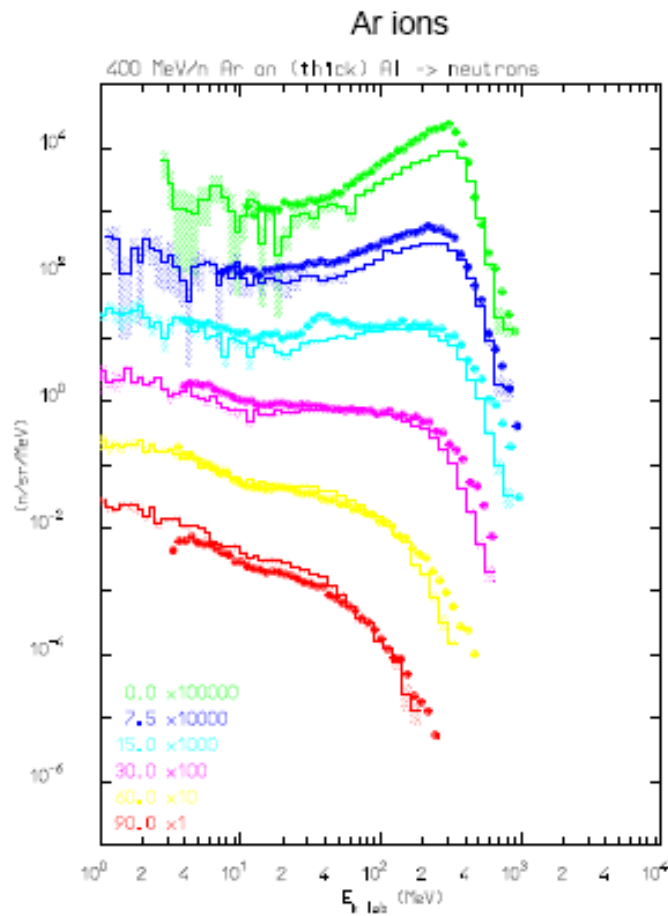


$$E_h = \frac{1}{2m_n} \left\{ \left[ p_{F0} (\rho(r)/\rho_0)^{1/3} \right]^2 - p^2 \right\}_{r, p(t=0)}$$

- fix the remaining energy-momentum conservation issues taking into account **experimental binding energies**
- use the FLUKA evaporation/fission/fragmentation module

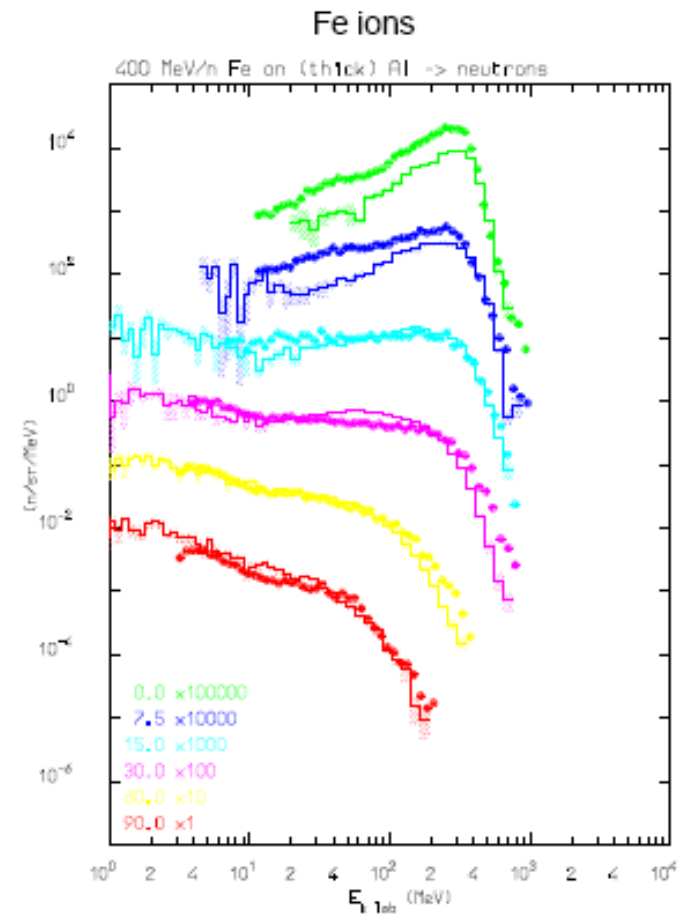
# RQMD - FLUKA benchmarks

## Double differential neutron yield



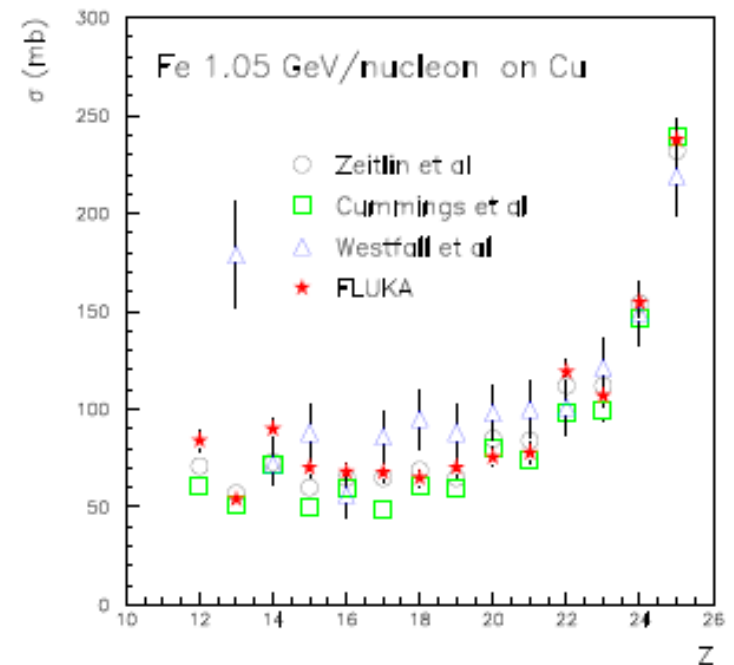
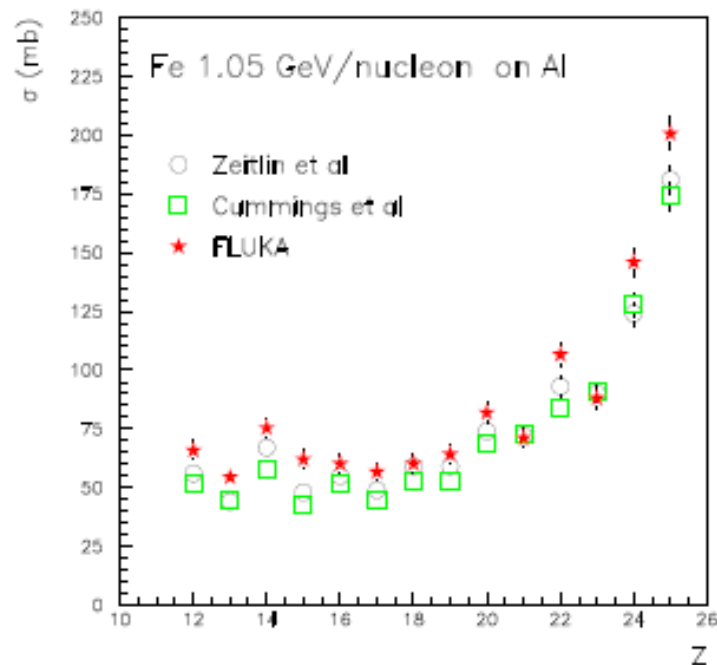
400 MeV/n

on *thick*  
Al targets



exp. data from T. Kurosawa *et al.*, Phys. Rev. C **62**, 044615 (2000)

## Fragment charge cross sections

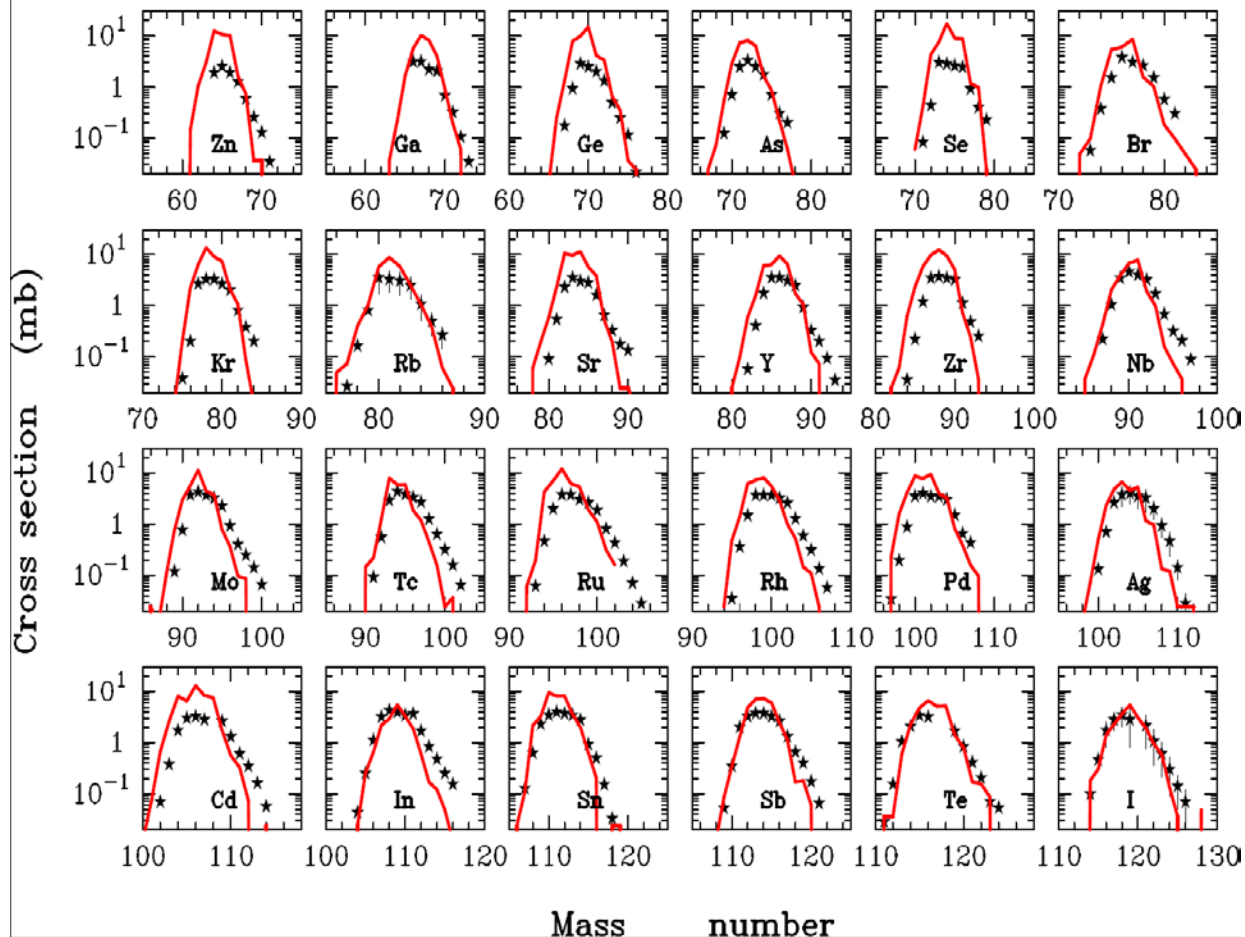


**exp. data** from C. Zeitlin *et al.*, Phys. Rev. **C 56**, 388 (1997),  
J.R. Cummings *et al.*, Phys. Rev. **C 42**, 2508 (1990) (at 1.5 GeV/n),  
G.D. Westfall *et al.*, Phys. Rev. **C 19**, 1309 (1979) (at 1.88 GeV/n)

# RQMD - FLUKA benchmarks

## Isotopic distributions of fragmentation products

$^{238}\text{U} + ^{208}\text{Pb}$  (750 A MeV)



*fission* products excluded  
like in the experimental  
analysis

exp. data (stars) from J. Benlliure, P. Armbruster *et al.*, Eur. Phys. J **A 2**, 193 (1998)



# BME

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## BME - *References*

interface to a Monte Carlo code  
founded on the BME theory (E. Gadioli et al.)

[M. Cavinato *et al.*, Nucl. Phys. **A 679**, 753 (2001),

M. Cavinato *et al.*, Phys. Lett. **B 382**, 1 (1996)]

## BME - *The interfaced code*

two different main reaction paths have been adopted:

### 1. COMPLETE FUSION

$$P_{CF} = \sigma_{CF} / \sigma_R$$

*composite nucleus formation*

### 2. PERIPHERAL COLLISION

$$P = 1 - P_{CF}$$

*three body mechanism with possible incomplete fusion  
one nucleon break-up and possibly transfer (at high  $b$ )  
pickup/stripping (for asymmetric systems at low  $b$ )*

**pre-equilibrium** de-excitation of the produced fragment(s)  
according to the BME theory (where available)  
or the PEANUT exciton model



*NB interface to PEANUT pre-eq  
not yet distributed!*

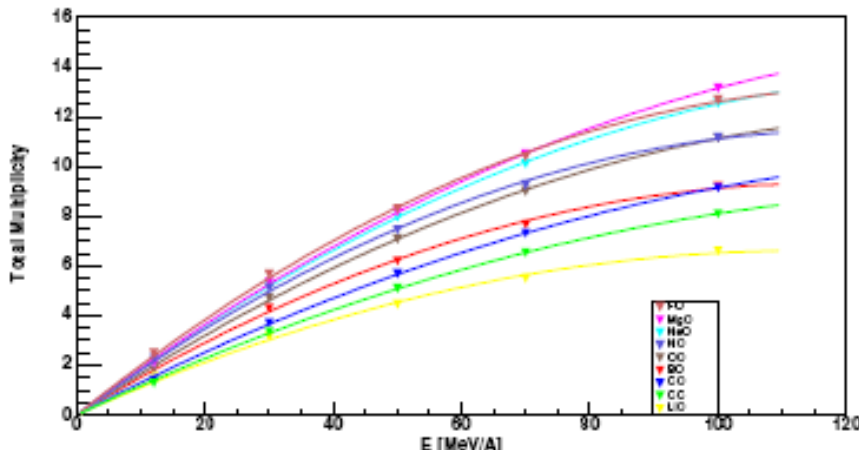
FLUKA evaporation/fission/fragmentation/gamma de-excitation

# BME - The database for the pre-equilibrium emissions

In order to get the multiplicities of the pre-equilibrium particles and their double differential spectra, the BME theory is applied to several representative systems at different bombarding energies and the results are parameterized.

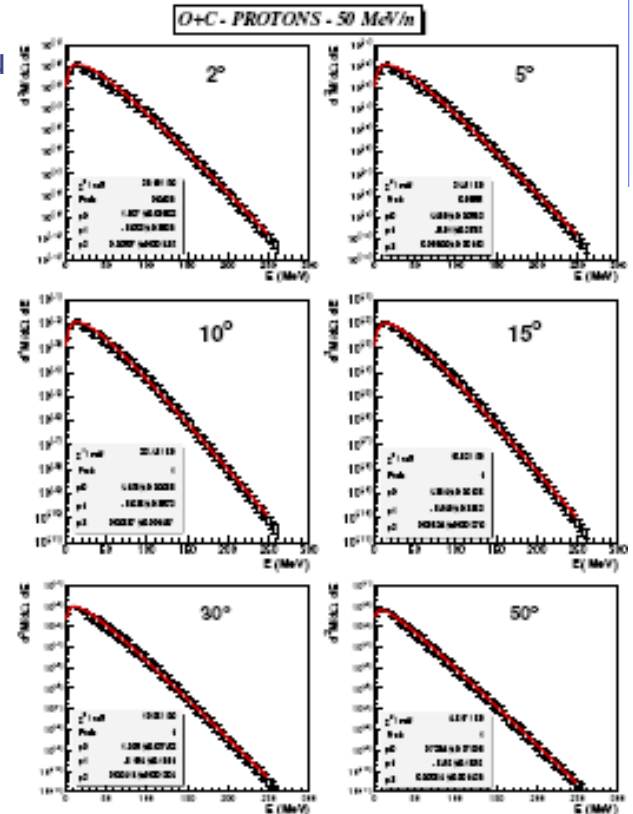


@ 12, 30, 50, 70, 100 MeV/n



total multiplicity

$$M = P_1 E_{nucl} - P_2 E_{nucl}^2$$



energy spectra

$$\frac{d^2M}{(dE d\Omega)} = E^{P_0(\theta)} \exp(-P_1(\theta) - P_2(\theta)E)$$

Work is ongoing to extend it to more massive systems, i.e.



and consequently review the fitting functions

and the extrapolation recipes over a significantly larger mass range

## BME - Theoretical framework

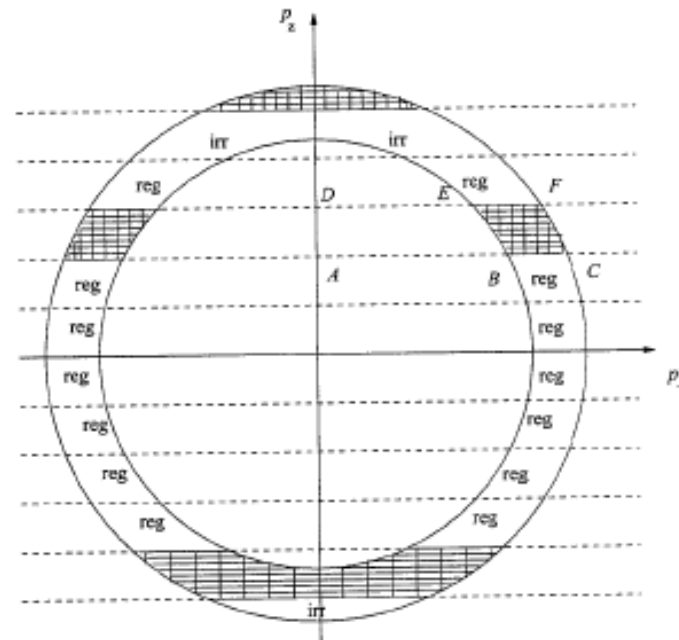
### Calculation of preequilibrium for the composite nucleus

proton and neutron momentum spaces divided into **bins**

$$\left\{ (p_x, p_y, p_z) : p_z \in [p_{zi}, p_{zi} + \Delta p_z), \varepsilon = (2m)^{-1} (p_x^2 + p_y^2 + p_z^2) \in [\varepsilon_i, \varepsilon_i + \Delta\varepsilon) \right\}$$

(**Z** is the beam direction)

of volume  $2\pi m \Delta\varepsilon \Delta p_z$



## BME - Theoretical framework

### The BME system

$$N_i = n_i g_i$$

nucleon number
occupation probability
number of states in bin  $i$

$$\begin{aligned}
 \frac{d(n_i^\pi g_i^\pi)}{dt} = & \sum_{jlm} [\omega_{lm \rightarrow ij}^{\pi\pi} g_i^\pi n_i^\pi g_m^\pi n_m^\pi (1 - n_i^\pi)(1 - n_j^\pi) \\
 & - \omega_{ij \rightarrow lm}^{\pi\pi} g_i^\pi n_i^\pi g_j^\pi n_j^\pi (1 - n_i^\pi)(1 - n_m^\pi)] \\
 + & \sum_{jlm} [\omega_{lm \rightarrow ij}^{\pi\nu} g_i^\pi n_i^\pi g_m^\nu n_m^\nu (1 - n_i^\pi)(1 - n_j^\nu) \\
 & - \omega_{ij \rightarrow lm}^{\pi\nu} g_i^\pi n_i^\pi g_j^\nu n_j^\nu (1 - n_i^\pi)(1 - n_m^\nu)] \\
 - & n_i^\pi g_i^\pi \omega_{i \rightarrow i'}^\pi g_{i'}^\pi \delta(\epsilon_i^\pi - \epsilon_{i'}^\pi - \epsilon_F^\pi - B^\pi) - \frac{dD_i^\pi}{dt}
 \end{aligned}$$

# BME - Theoretical framework

## Multiplicity spectra

of emitted nucleons

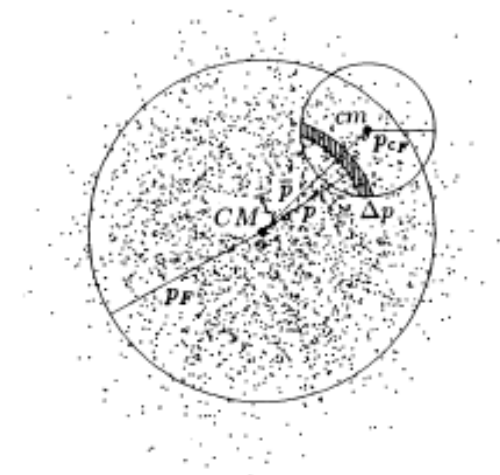
$$\frac{d^2 M(\varepsilon', \theta)}{d\varepsilon' d\Omega} = \frac{1}{2\pi \sin \theta} \int_0^{t_{eq}} n(\varepsilon, \theta, t) \frac{\sigma_{inv} V}{V} \rho(\varepsilon', \theta) dt$$

of a cluster  $c$

$$\frac{d^2 M_c(E'_c, \theta_c)}{dE'_c d\Omega} = \frac{R_c}{2\pi \sin \theta} \int_0^{t_{eq}} N_c(E_c, \theta_c, t) \frac{\sigma_{inv,c} V_c}{V} \rho_c(E'_c, \theta_c) dt$$

$$N_c(E_c, \theta_c, t) = \prod_i (n_i^\pi(\varepsilon, \theta, t))^{P_i(E_c, \theta_c) Z_c} \cdot \prod_i (n_i^\nu(\varepsilon, \theta, t))^{P_i(E_c, \theta_c) N_c}$$

joint probability



# BME - Peripheral collisions

We integrate the nuclear densities of the projectile and the target over their overlapping region, as a function of the impact parameter, and obtain a preferentially excited "middle source" and two fragments (projectile- and target-like). The kinematics is suggested by break-up studies.

## ii. kinematics determination

$\theta_{PL}$ ,  $\theta_{TL}$  chosen according to  $[d\sigma/d\Omega]_{cm} \sim \exp(-k\theta_{cm})$

$\theta_{MS}$  momentum conservation

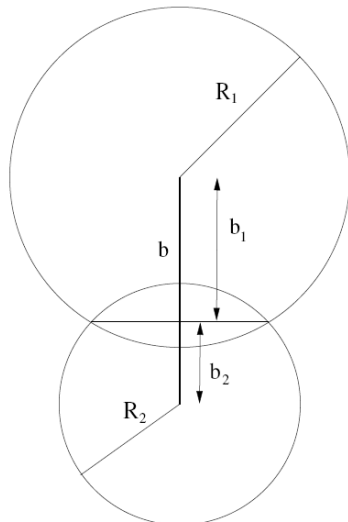
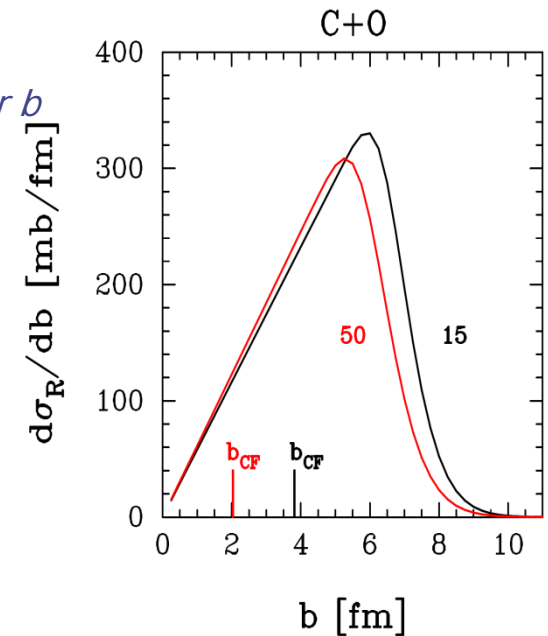
$p_{PL}$ ,  $p_{TL}$  chosen according to a given energy loss distribution

$p_{MS}$  momentum conservation

$\phi_{PL}$  free

$\phi_{TL}$ ,  $\phi_{MS}$  same reaction plane

## i. selection of the impact parameter $b$



## iii. excitation energy sharing

$$E_{MS}^* = (A_{MS}/A_{tot}) E_{tot}^* \sum_{n=0}^k (1 - A_{MS}/A_{tot})^n$$

$$E_{PL}^* = f(A_{PL}, A_{TL}) (E_{tot}^* - E_{MS}^*)$$

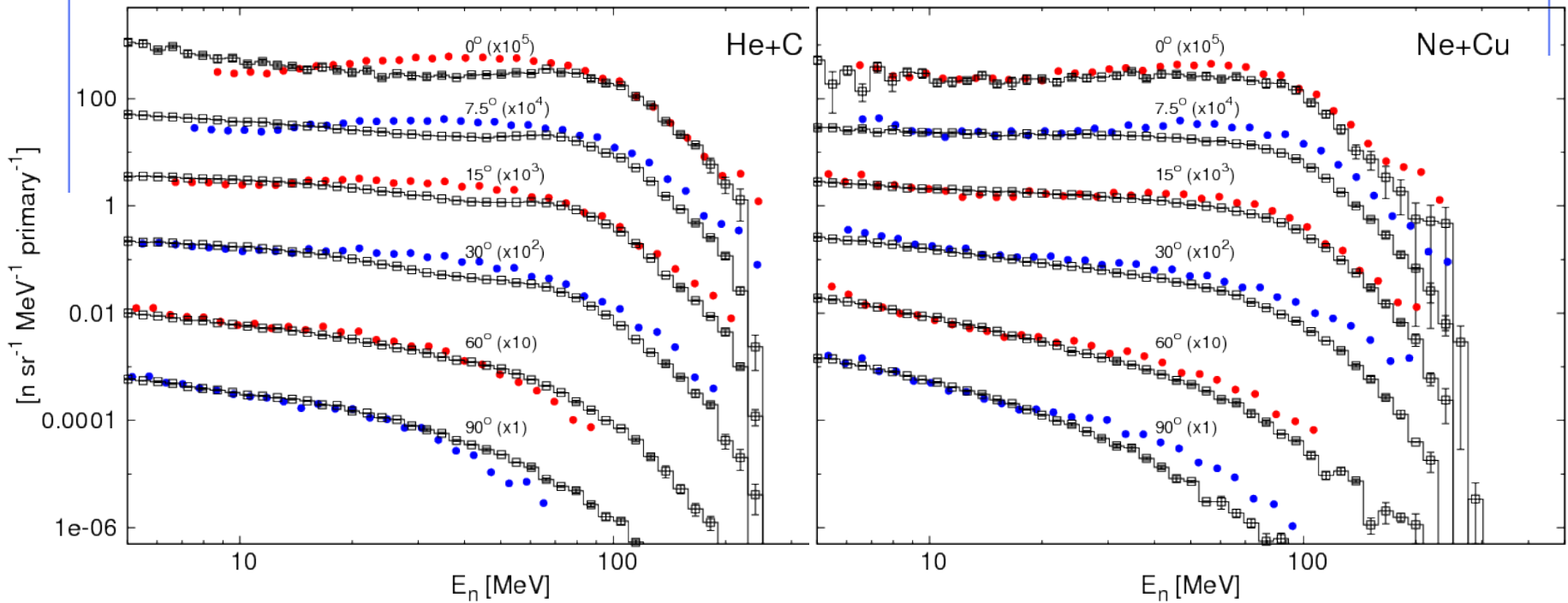
forced on the experimental values in the discrete level region

$$E_{TL}^* = (E_{tot}^* - E_{MS}^* - E_{PL}^*)$$



# BME - Benchmarking

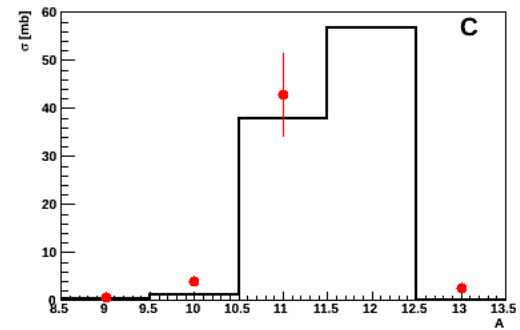
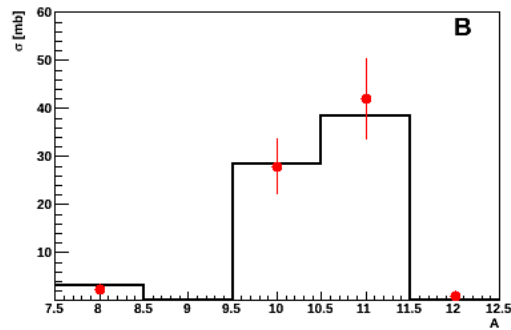
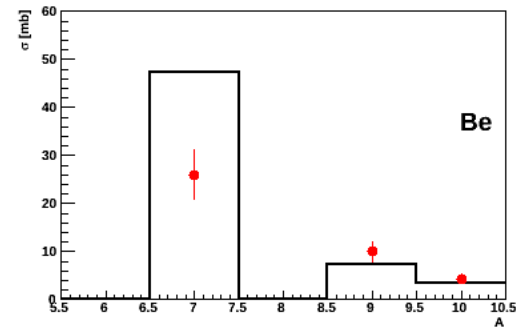
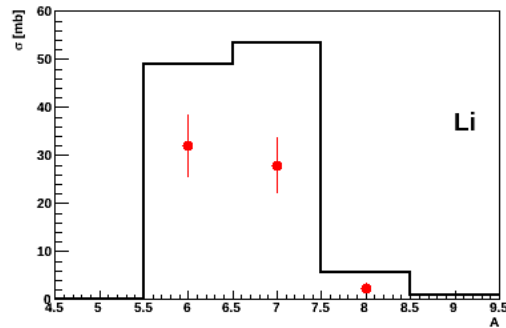
## DOUBLE DIFFERENTIAL NEUTRON YIELDS FROM 100 MeV/n BEAMS ON THICK TARGETS



FLUKA vs experimental data from T. Kurosawa, N. Nakao, T. Nakamura et al., Nucl. Sci. Eng. 132, 30 (1999)

# BME - Benchmarking

## ISOTOPE YIELDS FROM C+C at 86 MeV/n

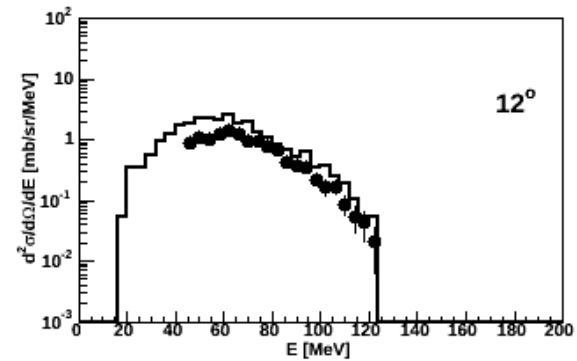
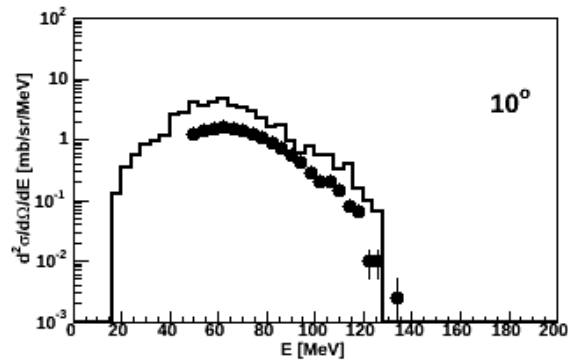


experimental data from H. Ryde, Physica Scripta T5, 114 (1983)

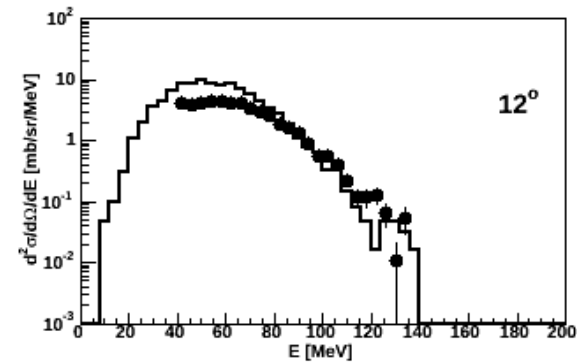
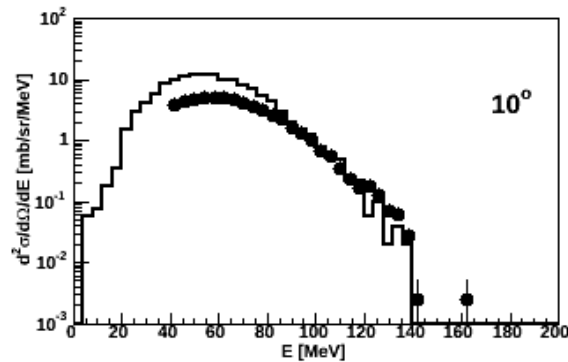
# BME - Benchmarking

## DOUBLE DIFFERENTIAL FRAGMENT SPECTRA FROM C+C at 13 MeV/n

Fluorine



Oxygen



experimental data by courtesy of S. Fortsch et al., iThemba Labs, South Africa

# Input options - 1

## a) define momentum / energy

```
BEAM          -10.0      0.0      0.0      0.0      0.0      0.0HEAVYION
```

WHAT(1) > 0.0 : average beam momentum (GeV/c)  
< 0.0 : average beam kinetic energy (GeV)

WHAT(2) beam momentum spread (GeV/c)

Note: for SDUM = HEAVYION units per nucleon (in fact per *nmu*)  
for SDUM = 4-HELIUM, etc. per nucleus

WHAT(3)-WHAT(6) (as for any other particle)

SDUM = HEAVYION

also      4-HELIUM    alpha  
          3-HELIUM    3-helium  
          TRITON     tritium  
          DEUTERON   deuterium

## Input options - 2

b) define charge and mass (*required for* BEAM/SDUM=HEAVYION)

HI-PROPE	79.0	197.0	0.0	0.0	0.0	0.0
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WHAT(1) = Atomic number Z of the heavy ion, Default: 6.0

WHAT(2) = Mass number A of the heavy ion, Default: 12.0

WHAT(3) = if < 0 isomeric state of the heavy ion

c) switch on heavy ion transport and interactions

IONTRANS	-2.0	<i>(pleonastic in case of ion beams)</i>
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*Note: Don't forget* to link the DPMJET/RQMD event generators for enabling ion-ion interactions above 125MeV/n either using FLAIR or `$FLUPRO/flutil/ldpmqmd`. The BME event generator, covering the low energy range up to 150MeV/n (125MeV/n is the default threshold, that you can change through PHYSICS/SDUM=DPMTHTRES), does not need to be linked since it's already embedded in the main FLUKA library

## Input options - 3

### Notes:

- The transport momentum threshold for ions ( $p_{th,HI}$ ) is fixed to that of alphas ( $p_{th,\alpha}$ )

$$p_{th,HI} = p_{th,\alpha} \times m_{HI}/m_{\alpha} \quad (GeV/c)$$

- Unless the transport threshold for alphas is defined with a PART-THR card (*requiring GeV and not GeV per nucleon*) it is set equal to 10 MeV  
if DEFAULTS=NEW-DEFA.
- When the energy of an ion becomes lower than the transport threshold, and if such threshold is lower than 100 MeV/n, the ion is not stopped, but it is ranged out to rest

## Input options - 4

### Electromagnetic dissociation

PHYSICS	2.0	0.0	0.0	0.0	0.0	0.0	EM-DISSO
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**WHAT(1) : flag for activating ion electromagnetic-dissociation**

=< -1.0 : resets to default (no em-dissociation)  
= 0.0 : ignored  
= 1.0 : (default) no em-dissociation  
= 2.0 : projectile and target em-dissociation activated  
= 3.0 : projectile only em-dissociation activated  
= 4.0 : target only em-dissociation activated

WHAT(2)-WHAT(6): not used